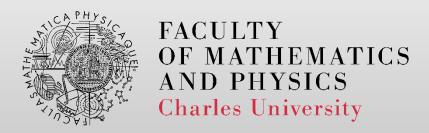
### **Abstraction**

http://d3s.mff.cuni.cz



Pavel Parízek



### Motivating example

```
int sum(int from, int to) {
 1:
 2:
       int total = 0;
 3:
       for (int i = from; i <= to; i++) {
4:
         total += i;
 5:
6:
       return total;
7:
8:
     main() {
9:
       int x = sum(1, 1000);
10:
       assert(x > 0);
11:
```

#### **Abstraction**



- Approaches
  - Reducing the size of variables' data domains
  - Ignoring concrete values of certain variables

- Benefits
  - Mitigating the state space explosion
  - Improved scalability (performance)



#### **Data abstraction**

- Using abstract domains for program variables
- Tracking only abstract states of the program

• Abstract state = set of concrete states

- Process: mapping concrete to abstract
  - data types, values, operations, program states



Pavel Parízek Abstraction

## **Example: Signs abstraction**

- Abstract data type
  - int → { NEG, ZERO, POS }

Q: What about values and operations? Let's consider only addition here.



## **Example: Signs abstraction**

- Abstract data type
  - int → { NEG, ZERO, POS }
- Abstract values
  - $\blacksquare$   $\alpha(x) \subseteq \{ NEG, ZERO, POS \}$
- Abstract operation +

	NEG	ZERO	POS
NEG	{ NEG }	{ NEG }	{ NEG, ZERO, POS }
ZERO	{ NEG }	{ ZERO }	{ POS }
POS	{ NEG, ZERO, POS }	{ POS }	{ POS }

### Construction of abstract programs

Transformation of program source code

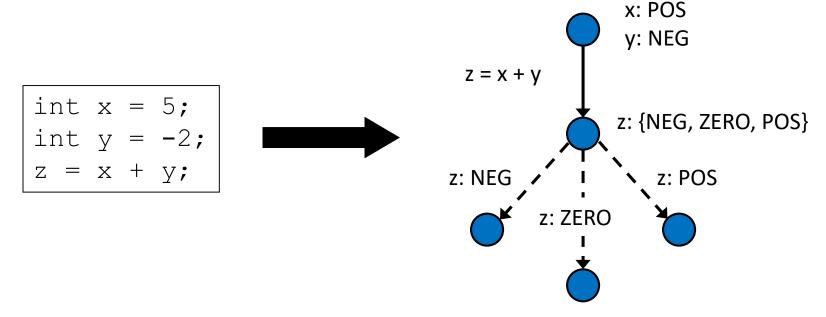
```
int x = 0;
...
int y;
y = x + 2;
```



```
Signs x = Signs.ZERO;
...
Signs y;
y = Signs.add(x, Signs.POS);
```

## **Abstract state space**

- Non-deterministic choice
  - assignment, branching condition (if-else, loops)





## Other simple data abstractions



- Interval abstraction
  - **Example:**  $x < 0, 0 \le x \le 10, x > 10$

- Combining intervals with concrete values
  - **Example:** x < 0, x = 0, x = 1, x = 2, x = 3, x = 4, x > 4

### **Predicate abstraction**



### **Predicate abstraction**



- Predicates about program variables
  - Theories: linear integer arithmetic, equality, arrays
  - **•** Example: x = 0, x > 0, y + z ≥ 2, u = v, select(a,1) = 5
- Abstract state
  - Some valuation of all the predicates

### **Example**

```
int sum(int from, int to) {
2:
      int total = 0;
3:
      for (int i = from; i <= to; i++) {
4:
        total += i;
5:
6:
     return total;
7:
8: int x = sum(1, 1000);
9: assert (x > 0);
```

#### Q: what predicates should we use here?



### **Boolean program**

```
bool P1 = false;
bool P2 = false;
// int total = 0;
P2 = true;
// int i = from;
P1 = *;
// total += i;
if (P1 \&\& P2) P2 = true;
else P2 = *;
```

#### **Predicates**

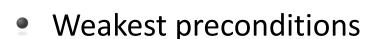
P1: i > 0

P2: *total* ≥ 0



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### **Deriving predicate valuations**



- Predicate p: total  $\geq 0$
- Statement s: total += i;
- WP(s,p)  $\equiv$  total + i  $\geq$  0
- Querying the SMT solver
  - Example: p1 && !p2  $\rightarrow$  WP(s,p) is valid?
- Processing results
  - 1) p1 && !p2  $\rightarrow$  WP(s,p) is valid  $\rightarrow$  if (p1 && !p2) p = true;
  - 2) p1 && !p2  $\rightarrow$  WP(s,!p) is valid  $\rightarrow$  if (p1 && !p2) p = false;
  - 3) both valid or none valid  $\rightarrow$  if (p1 && !p2) p = \*;



### **Optimizations**

Goal: reduce the number of queries for SMT

- Possible approaches
  - Compute new valuation only for predicates that refer to variables modified by the given concrete assignment statement
    - We must be very careful though: aliasing
  - For generating branches of the big if-else statements in the abstract boolean program, consider only predicates that refer to variables read by the assignment statement



### Verification using predicate abstraction

- Using model checker for boolean programs
  - Much easier task than for general programs (C, Java)
  - Well-known optimizations: symbolic model checking

- Practical challenges
  - Translating counterexamples back to source code
  - Encoding properties into reachability of assertions

### **Abstraction: characteristics**



Distributed and Dependable

#### **Abstraction: characteristics**

Assume that we want to verify a given program.

Q: What important characteristic should the abstract program have ?



### **Over-approximation**

- Abstract program captures all possible behaviors of the original concrete program
  - Behavior: possible control flow path, thread interleaving
- Purpose: complete verification (all reachable states)
- Examples
  - Simple data abstraction
  - Predicate abstraction
- Problem: imprecise abstraction
  - Captures some infeasible execution paths spurious errors
  - Branch conditions replaced with a non-deterministic choice

#### **Abstraction: characteristics**

Q1: Is there some other way to creating abstract programs than over-approximation?

Q2: If yes, when does it make sense to use it?

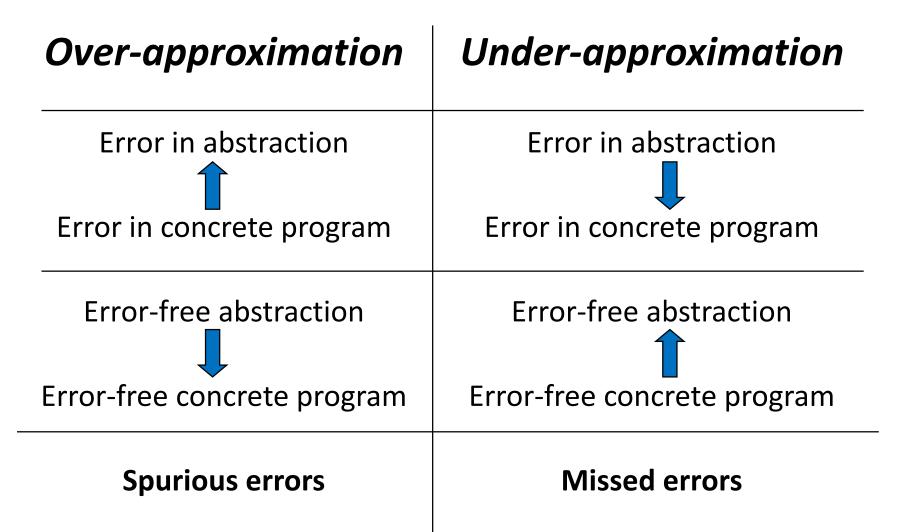


### **Under-approximation**

- Abstract program captures only a certain subset of all possible behaviors of the concrete program
  - selected thread interleavings, reduced data domains
- Purpose: fast error detection (subset of reachable states)
- Examples
  - Normal tests (used in SW industry)
  - State space traversal with heuristics
  - Context-bounded search (traversal)
  - Bounded model checking in general
- Problem: imprecise abstraction
  - Omits some feasible execution paths missed errors



#### **Abstractions: characteristics**





Pavel Parízek Abstraction 22

#### **Abstraction: issues**

- Very hard to get right
  - Too precise → state explosion
  - Too coarse → spurious errors

- Possible remedy
  - Start with coarse abstraction
  - Employ iterative refinement



### **CEGAR**



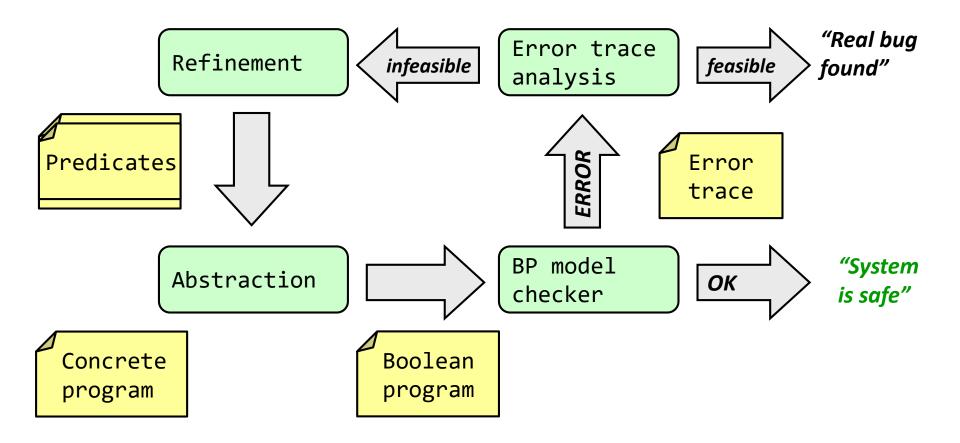
#### **CEGAR**



Counter-Example Guided Abstraction Refinement

Automated iterative refinement based on spurious errors

#### **CEGAR**





## Challenges



Inferring additional predicates

### **Checking error trace feasibility**

- Simulate the abstract error trace on the concrete program
- Record the path condition PaC using symbolic execution
  - Options selected at choice points (if-else, loops, non-determinism)
- Create path formula that encodes the whole error trace
  - The assume statement: clauses from the PaC (selected branches)
- Check satisfiability of the path formula (query the SMT solver)

- Example
  - Error trace

```
index = 1; total = total + index; assume index > 1000
```

Path formula

```
(index0 = 1) \&\& (total1 = total0 + index0) \&\& (index0 > 1000)
```

## Inferring additional predicates

- Divide path formula φ into two parts φ<sup>-</sup> and φ<sup>+</sup>
  - such that  $\phi^-$  &&  $\phi^+$  is unsatisfiable
- Then derive a Craig interpolant ψ for φ<sup>-</sup> and φ<sup>+</sup>
  - Logic formula ψ such that
    - $\Phi^- \rightarrow \Psi$ ,  $\Phi^+ \&\& \Psi$  is unsatisfiable, and
    - $\psi$  uses symbols common to  $\varphi^-$  and  $\varphi^+$
- Finally generate additional predicates from ψ

#### Example

- Path formula
  - (index0 = 1) && (total1 = total0 + index0) && (index0 > 1000)
- $\bullet$   $\bullet$ : index0 = 1 && total1 = total0 + index0
- $\phi^+$ : index0 > 1000
- $\psi$ : index0 = 1 // newly inferred predicate in this case
- Disclaimer
  - Bad choices of inferred predicates may lead to non-termination
  - Tools generate predicates that may look strange (not intuitive)



# **SLAM/SDV**

- Static Driver Verifier (SDV)
  - SLAM: verification engine that uses CEGAR
- Purpose
  - Analyzing third party Windows device drivers
    - Specific rules about proper usage of Windows kernel API
    - Major source of kernel crashes (infamous "blue screens")
    - Drivers have feasible code size and a strict environment
- Many extensions developed in the last decade
- Additional information
  - https://www.microsoft.com/en-us/research/project/slam/
  - Many research papers, slides, download, user guides



### **Optimizations**

- Lazy abstraction
  - Set of predicates specific to each code location
  - Tools: BLAST

- Method summaries
  - Logic formula relating inputs and outputs
  - Summaries computed using interpolants
  - Tools: Whale, FunFrog, ...



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#### **Tools**

- BLAST
  - https://www.sosy-lab.org/~dbeyer/Blast/index-epfl.php
- CPAchecker
  - http://cpachecker.sosy-lab.org/
- UFO/Whale
  - https://bitbucket.org/arieg/ufo/wiki/Home
- Wolverine
- ... and many others



### **Further reading**

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