Static Analysis: Overview, Data-Flow

http://d3s.mff.cuni.cz



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Static analysis

Purpose

Gather information about run-time behavior of programs without executing them

Information

- Does the variable x have a constant value?
- Is the value of the variable x always positive?
- May the pointer p be null at a code location?
- What are possible values of the variable y?

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Static analysis: characteristics

- Target model of program behavior
 - some kind of *Control Flow Graph* (CFG)
- Provides approximate answers
 - Decision problems: yes / no / don't know
 - Collecting some values: superset / subset
- Information valid for all possible runs
- Summarizing different execution paths
 - branches of the if-else statement, loop iterations
- Does not know run-time values (inputs)

Comparison

Static analysis

control-flow graph

summarizes information from different paths

approximation

scalability

Model checking

program state space

reasons about execution paths independently

path-sensitivity

precision

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Static analysis in practice

Optimizing compilers

- Detect superfluous evaluations of the same expression
- Detect unused local variables or dead code fragments

- Program verification
 - Search for possible runtime errors
 - Example: null pointer dereference, unsynchronized access
 - Constructing abstraction for model checking
 - Slicing: identify statements irrelevant for a given property

Approximation

Q: What important restrictions there are?



Restrictions

- Approximation must be safe
 - That precisely means "imprecise on the safe side"
- Target domain: optimizing compilers
 - Under-approximation
 - Optimization performed on the basis of analysis results must not violate semantics of a given program
 - Example: constant propagation
 - Sound analysis identifies a program variable as a constant only when it is really certain (100%)

Restrictions

- Approximation must be safe
 - That precisely means "imprecise on the safe side"
- Target domain: search for errors
 - Over-approximation
 - Safe analysis reports all real errors and also some spurious errors (false positives)
 - Example: possible null dereferences
 - We want to know about all of them so we can add runtime checks (if (v != null) ...)

Basic concepts (theory and examples)



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Running example

```
Program
    int factorial(int n) {
      int r;
      if (n == 0) r = 0;
      int f = 1;
      while (n > 0) {
        f = f * n;
        n = n - 1;
        if (n == 0) r = f;
      }
      return r;
    }
```

Static analysis: possibly uninitialized variables

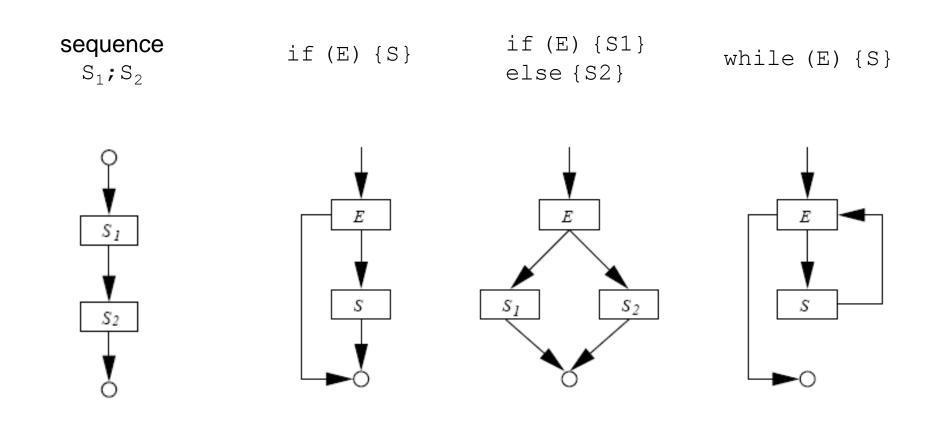


Control flow graph (CFG)

- Directed graph with labels
- Nodes: program points (statements)
- Edges: possible flow of control
 - pred(n) and succ(n) for each node n in a CFG
- Single point of entry
- Single point of exit

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CFG: modeling control structures





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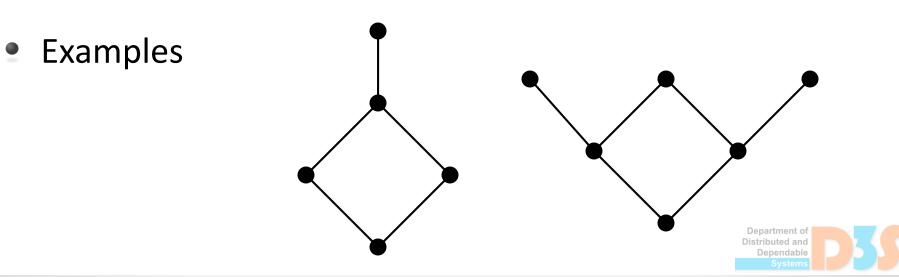
Set of possible values (facts)

Finite lattice over the set



Partial order

- Mathematical structure $L = (S, \sqsubseteq)$
 - S is a set of values (e.g., analysis facts)
 - is a binary relation (e.g., is-subset)
 - Reflexivity: $\forall x \in S : x \sqsubseteq x$
 - Transitivity: $\forall x, y, z \in S : x \sqsubseteq y \land y \sqsubseteq z \Rightarrow x \sqsubseteq z$
 - Anti-symmetry: $\forall x, y \in S : x \sqsubseteq y \land y \sqsubseteq x \Rightarrow x = y$



Bounds

Lets have a partial order $L = (S, \sqsubseteq)$ and $X \subseteq S$

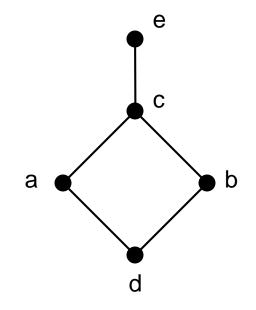
- Upper bound
 - $y \in S$ is an upper bound for X, i.e. $X \sqsubseteq y$, if $\forall x \in X : x \sqsubseteq y$
- Lower bound
 - $y \in S$ is a lower bound for X, i.e. $y \sqsubseteq X$, if $\forall x \in X : y \sqsubseteq x$
- Least upper bound of *X*, denoted as $\sqcup X$

 $X \sqsubseteq \sqcup X \land \forall y \in S : X \sqsubseteq y \Rightarrow \sqcup X \sqsubseteq y$

- Greatest lower bound of X, denoted as $\Box X$
 - $\square X \sqsubseteq X \land \forall y \in S : y \sqsubseteq X \Rightarrow y \sqsubseteq \Box X$

Lets have a partial order $L = (S, \sqsubseteq)$ and the set $S = \{a, b, c, d, e\}$

The upper bounds of $X = \{a, b\}$ are the elements $\{c, e\}$

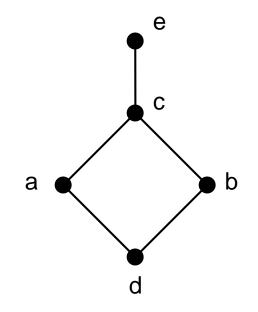


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Lets have a partial order $L = (S, \sqsubseteq)$ and the set $S = \{a, b, c, d, e\}$

The greatest lower bound of $X = \{b, e\}$ is the element b



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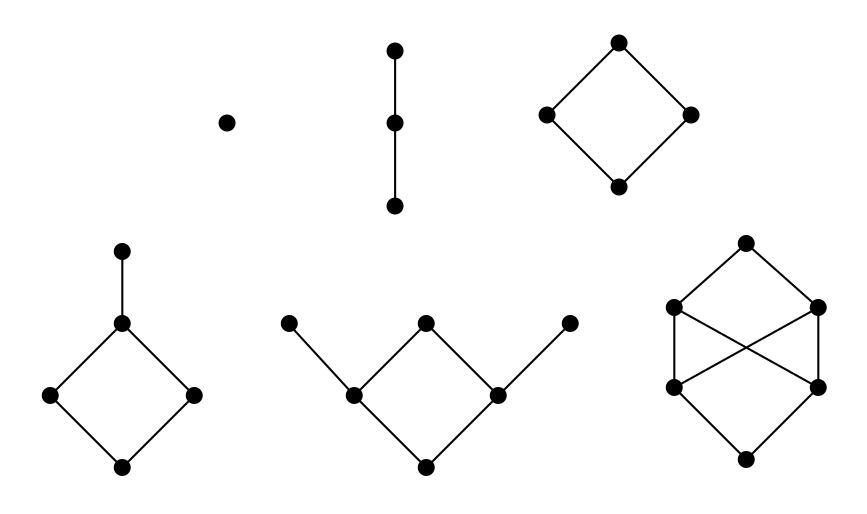
Lattice

- Partial order $L = (S, \sqsubseteq)$ such that
 - $\blacksquare \ \sqcup X \text{ and } \Pi X \text{ exist for } \forall X \subseteq S$
 - Unique greatest element $\top = \Box S = \Box \emptyset$
 - Unique least element $\perp = \Box S = \Box \emptyset$
- Height of a lattice
 - Length of the longest path from \perp to \top



- Partial order $L = (S, \sqsubseteq)$ such that
 - $\forall x, y \in S$ there is
 - Least upper bound x ⊔ y
 - Greatest lower bound $x \sqcap y$

Lattice: examples



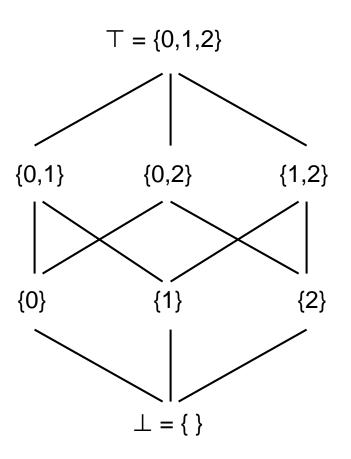


Using finite lattices in static analysis

- Lattice $L = (S, \Box)$
 - Set S of analysis facts (units of information)
 - Relation Gefines an ordering with respect to precision of the abstraction
 - $x \sqsubseteq y \Rightarrow x$ is more precise than y
 - $x \sqsubseteq y \Rightarrow y$ approximates x
 - Example
 - Sign abstraction: x = { POS }, y = { POS, ZERO }

How to construct lattices

- Finite set R induces a lattice $(2^R, \sqsubseteq)$
 - ∎ ⊥ = ⊔Ø
 - No information available
 - $\top = R$
 - Any possible value
 - $x \sqcup y = x \cup y$
 - 🔋 join
 - $x \sqcap y = x \cap y$ • meet
 - Height |R|
- Example
 - Set R = {0, 1, 2}
 - Height = 3





Running example

```
Program
    int factorial(int n) {
      int r;
      if (n == 0) r = 0;
      int f = 1;
      while (n > 0) {
        f = f * n;
        n = n - 1;
        if (n == 0) r = f;
      }
      return r;
    }
```

Static analysis: possibly uninitialized variables



Encoding program statements

- Data for each node in the CFG
 - IN: valid before the program statement
 - OUT: valid after the program statement
- Merge operator L
 - CFG nodes with multiple predecessors
 - Typical approach: union or intersection

Transfer functions

For each node in CFG (statement), we must define a transfer function
 OUT = (IN \ kill) U gen

- Examples
 - Statement int r;

Statement r = f;



Monotone functions

- Function $f: S \rightarrow S$ is monotone if
 - $\forall x, y \in S : x \sqsubseteq y \Rightarrow f(x) \sqsubseteq f(y)$

- Examples
 - Constant functions
 - Operators П and Ц
 - Their compositions



Computing static analysis

- Input
 - Control flow graph of the given program
 - Initial value for each CFG node (\perp or \emptyset)
 - Value is the set of known analysis facts (information)
 - Merge operator defined as the set union
 - Transfer functions F_i for each node in CFG
- Approach: compute fixed points
 - Information associated with the CFG nodes

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Duality

• We focus just on \sqsubseteq and initial values \bot



Computing fixed points

- Motto: "walk up the lattice starting at \perp , until you reach a fixed point"
 - In the worst case, \top is the fixed point (if exists)

- Three algorithms
 - Naive (brute force)
 - Chaotic iteration
 - Worklist algorithm



Worklist algorithm

$$u_{1} = \pm; ..., u_{n} = \pm;$$

$$q = [1, ..., n];$$

while $(q \neq []) \{$
 $i = head(q);$
 $v_{IN} = merge(pred(i));$
 $v_{OUT} = F_{i}(v_{IN});$
 $q = tail(q);$
if $(v_{OUT} \neq u_{i}) \{$
 $append(q, succ(i));$
 $u_{i} = v_{OUT};$
}

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Classification



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Static analysis categories

Data-flow analysis

- Call graph construction
- Pointer analysis (aliasing)
- Escape analysis (threads)
- Side effect analysis



- Available expressions
- Reaching definitions
- Live variables (values)





Direction

Forward analysis

- Computes information about the past behavior
- Starts at the entry node (CFG) and goes forward

Backward analysis

- Computes information about the future behavior
- Starts at the exit CFG node and moves backwards

Approximation level

May analysis

- Computes information that may be true (over-approximation)
 - Information for P that is true at least for one path coming into P
- Merge operator: set union

Must analysis

- Computes information that must be true (under-approximation)
 - Information for P that is true for all execution paths coming into P
- Merge operator: set intersection

Flow sensitivity

- Flow-sensitive analysis
 - Considers the program's control flow (CFG) and the order of individual statements
 - Example: available expressions
- Flow-insensitive analysis
 - Program seen as an unordered collection of statements
 - Results are valid for any order of program statements
 - *S1*; *S2* versus *S2*; *S1*
 - Example: type analysis (inference)



- Intra-procedural
 - Every single procedure analyzed separately
 - Maximally pessimistic assumptions about side effects of procedure calls

- Inter-procedural
 - Whole program analyzed together
 - Sometimes without libraries (huge)

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Context sensitivity

- Context-sensitive analysis
 - Call site: source code location for the call
 - Call stack: procedure calls and returns
 - Receiver objects for method calls ("this")
 - Analysis results for the method M depend on the specific caller of M

- Context-insensitive analysis
 - Same analysis results for every call site of M



Tools

- WALA
 - Java, JavaScript, JVM (bytecode)
 - <u>https://wala.github.io/</u>
 - <u>https://github.com/wala</u>
- Soot
 - Java, JVM-based languages (bytecode)
 - <u>https://soot-oss.github.io/soot/</u>
- CIL
 - Only for programs written in C
 - http://www.cs.berkeley.edu/~necula/cil/
 - <u>https://github.com/cil-project/cil</u>
- LLVM
 - C, C++, Objective-C
 - Clang static analyzer
 - <u>http://llvm.org/</u>
- Roslyn: .NET compiler platform
 - <u>https://github.com/dotnet/roslyn</u>



- M. Schwartzbach. Lecture Notes on Static
 Analysis. Department of CS, Aarhus University
- A. Møller and M. Schwartzbach. Static Program Analysis. Department of CS, Aarhus University

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 Principles of Program Analysis. Springer, 2005

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