

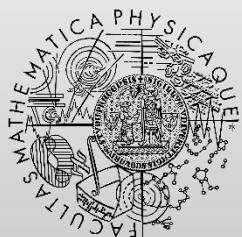
# Temporal Logics

<http://d3s.mff.cuni.cz>

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Systems



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# Modal logic



- Possibly

- $\Diamond P$

- Necessarily

- $\Box P$

# Dynamic logic



- Formulas
  - $\langle a \rangle P$
  - $[a] P$
- Special actions
  - Constant:  $[1] P$
  - Block:  $[0] P$

# Temporal logic



- Variants: LTL, CTL, ...
- Operators
  - Globally:  $G p$
  - Eventually:  $F p$
  - Next step:  $X p$
- Details: course NSWI101

# TLA: Temporal Logic of Actions



- TLA+ specification language
  - Low-level language based on logic and sets
  - Enables users to define a transition system
- PlusCal algorithm language
  - Syntax much closer to C/C#/Java
  - Writing and testing pseudo-code
- Home page
  - <http://lamport.azurewebsites.net/tla/tla.html>
- TLA Toolbox (IDE)
  - <http://lamport.azurewebsites.net/tla/tools.html>



- Features
  - control-flow statements, non-determinism, simple identification of atomic steps (for concurrency), procedure call and return
- Example algorithms
  - Euclid's GCD, mutual exclusion, alternating bit
- Translation into TLA+ specification
- Analyzing with TLC model checker
- Further reading
  - L. Lamport. **The PlusCal Algorithmic Language**. ICTAC 2009
    - <http://lamport.azurewebsites.net/pubs/pubs.html#pluscal>



- Features
  - variables, constants, arithmetic
  - common set and logic operators
  - functions, control statements
  - sequences, tuples, arrays, records
  - non-deterministic choice
  - basic temporal operators
- Example translation: Euclid's GCD
- Further reading
  - L. Lamport. **Euclid Writes an Algorithm: A Fairytale**
    - <http://lamport.azurewebsites.net/pubs/pubs.html#euclid>

# Advanced topics



- Liveness (termination)
- Fairness (scheduling)
- See the course NSWI101
  - <http://d3s.mff.cuni.cz/teaching/nswi101>

# Practice



- Analyzing distributed concurrent algorithms, protocols and systems
- Case study: Amazon
  - C. Newcombe, T. Rath, F. Zhang, B. Munteanu, M. Brooker, and M. Deardeuff. **How Amazon Web Services Uses Formal Methods.** Communications of the ACM, 58(4), April 2015
  - <http://doi.acm.org/10.1145/2699417>