

Advancements in User Interface and Usability of KeY

Wolfram Pfeifer | September 12, 2023



Deductive verifier for (sequential) Java



Deductive verifier for (sequential) Java
Java Modeling Language (JML)



Deductive verifier for (sequential) Java
Java Modeling Language (JML)
Modular specification/verification



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus

Symbolic Execution



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus

Symbolic Execution

Dynamic Frames



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus

Symbolic Execution

Dynamic Frames

Automatic and interactive application of rules



Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification



Dynamic Logic (JavaDL), sequent calculus

Symbolic Execution

Dynamic Frames

Automatic and interactive application of rules

Optional translation to SMT-LIB

Deductive verifier for (sequential) Java

Java Modeling Language (JML)

Modular specification/verification

Dynamic Logic (JavaDL), sequent calculus

Symbolic Execution

Dynamic Frames

Automatic and interactive application of rules

Optional translation to SMT-LIB

Counterexample generation

Information flow proofs

Testcase generation

...



Key 2.11.0
⌵ ⌵ ⌵

File View Proof Options Origin Tracking
About

Run CVC5, Princess, Z3
⏪ ⏩
📁 📄 📧 📧 📧 📧 📧
Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@4:49:20 PM

SumAndMaxSumAndMaxsumAndMax

Proof Search Strategy

Proof

Proof Tree

0: OPEN GOAL

Show taclet info (inner nodes only)

Sequent

Current Goal

```

=>
wellFormed(heap)
^ ~self = null
^ self.<created> = TRUE
^ SumAndMax::exactInstance(self) = TRUE
^ (a = null ∨ a.<created> = TRUE)
^ measuredByEmpty
^ ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → 0 ≤ a[i])
  ^ (self.<inv> ∧ ~a = null))
- {heapAtPre:=heap || ~a:=a}
  \<{
    exc=null;try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  }
  \> ( ∨ int i;
    ( 0 ≤ i ∧ i < a.length ∧ inInt(i)
      → a[i] ≤ self.max)
    ^ ( ( a.length > 0
      → ∃ int i;
        ( 0 ≤ i
          ^ i < a.length
          ^ inInt(i)
          ^ self.max = a[i])
        ^ ( self.sum
          = (int)(bsum(int i);(0, a.length, a[i]))
          ^ ( self.sum
            ≤ javaMulInt(a.length, self.max)
            ^ self.<inv>)))
    ^ exc = null
    ^ ∨ Field f;
      ∨ java.lang.Object o;
      ( (o, f) ∈ {(self, SumAndMax::$sum)}
        ∪ {(self, SumAndMax::$max)})
      ∨ ~o = null
      ^ ~o.<created>@heapAtPre = TRUE
      ∨ o.f = o.f@heapAtPre)
  
```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures (∑sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23     @ && (k == 0 ==> max == 0)
24     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (∑sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable sum, max;
29     @ decreases a.length - k;
30     @*/
31     while(k < a.length) {
32       if(max < a[k]) {
33         max = a[k];
34       }
35       sum += a[k];
36       k++;
37     }
38   }
39 }
40
  
```

Show Postcondition/Assignable

Proof has been pruned: one open goal remains.
Show log

Key 2.11.0
About

File View Proof Options Origin Tracking
Run CVC5, Princess, Z3
Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@4:49:20 PM

SumAndMaxSumAndMaxsumAndMax

Proof Search Strategy

Proof

Proof Tree

0: OPEN GOAL

Show tactic info (inner nodes only)

Sequent

Current Goal

precondition ϕ

```

wellFormed(heap)
  A ~self = null
  A self.<created> = TRUE
  A SumAndMax::exactInstance(self) = TRUE
  A (a = null  $\vee$  a.<created> = TRUE)
  A measuredByEmpty
  A (  $\forall$  int i; (0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)  $\rightarrow$  0  $\leq$  a[i])
    A (self.<inv>  $\wedge$  ~a = null))
  - {heapAtPre:=heap || ~a:=a}
  \<{
    exc=null;try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  }
  \> (  $\forall$  int i;
    ( 0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)
       $\rightarrow$  a[i]  $\leq$  self.max)
    A ( ( a.length > 0
       $\rightarrow$   $\exists$  int i;
        ( 0  $\leq$  i
          A i < a.length
          A inInt(i)
          A self.max = a[i])
        A ( self.sum
          = (int)(bsum(int i);(0, a.length, a[i]))
          A ( self.sum
             $\leq$  javaMulInt(a.length, self.max)
            A self.<inv>)))
    A exc = null
    A  $\forall$  Field f;
       $\forall$  java.lang.Object o;
        ( (o, f)  $\Leftarrow$  ((self, SumAndMax::$sum)
          U ((self, SumAndMax::$max))
           $\vee$  ~o = null
          A ~o.<created>@heapAtPre = TRUE
           $\vee$  o.f = o.f@heapAtPre))
          
```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7   @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8   @ assignable sum, max;
9   @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10  @ ensures (a.length > 0
11  @ ==> (\existsits int i; 0 <= i && i < a.length; max == a[i]));
12  @ ensures (sum == (\sum int i; 0 <= i && i < a.length; a[i]));
13  @ ensures sum <= a.length * max;
14  @*/
15 void sumAndMax(int[] a) {
16   sum = 0;
17   max = 0;
18   int k = 0;
19
20   /*@ loop_invariant
21   @ 0 <= k && k <= a.length
22   @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23   @ && (k == 0 ==> max == 0)
24   @ && (k > 0 ==> (\existsits int i; 0 <= i && i < k; max == a[i]))
25   @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26   @ && sum <= k * max;
27   @
28   @ assignable sum, max;
29   @ decreases a.length - k;
30   @*/
31   while(k < a.length) {
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39 }
40
          
```

Show Postcondition/Assignable

Proof has been pruned: one open goal remains.
Show log

Key 2.11.0
About

File View Proof Options Origin Tracking
Run CVC5, Princess, Z3
Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@4:49:20 PM

SumAndMaxSumAndMaxSumAndMax

Proof Search Strategy

Proof

Proof Tree

0: OPEN GOAL

Show taclet info (inner nodes only)

Sequent

Current Goal

precondition ϕ

```

wellFormed(heap)
 $\wedge$  self = null
 $\wedge$  self.<created> = TRUE
 $\wedge$  SumAndMax::exactInstance(self) = TRUE
 $\wedge$  (a = null  $\vee$  a.<created> = TRUE)
 $\wedge$  measuredByEmpty
 $\wedge$  (  $\forall$  int i; (0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)  $\rightarrow$  0  $\leq$  a[i])
 $\wedge$  (self.<inv>  $\wedge$  !a = null))

```

```

- {heapAtPre:=heap || !_a:=a}
\<{
exc=null;try {
self.sumAndMax(_a)@SumAndMax;
} catch (java.lang.Throwable e) {
exc=e;
}
}\> (  $\forall$  int i;
( 0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)
 $\rightarrow$  a[i]  $\leq$  self.max)
 $\wedge$  ( ( a.length > 0
 $\rightarrow$   $\exists$  int i;
( 0  $\leq$  i
 $\wedge$  i < a.length
 $\wedge$  inInt(i)
 $\wedge$  self.max = a[i])
 $\wedge$  ( self.sum
= (int)(bsum(int i);(0, a.length, a[i]))
 $\wedge$  ( self.sum
 $\leq$  javaMulInt(a.length, self.max)
 $\wedge$  self.<inv>)))
 $\wedge$  exc = null
 $\wedge$   $\forall$  Field f;
 $\forall$  java.lang.Object o;
( (o, f)  $\in$  ((self, SumAndMax::$sum)
 $\cup$  ((self, SumAndMax::$max))
 $\vee$  !o = null
 $\wedge$  !o.<created>@heapAtPre = TRUE
 $\vee$  o.f = o.f@heapAtPre))

```

program p

Source

```

1 class SumAndMax {
2
3     int sum;
4     int max;
5
6     /*@ normal_behaviour
7     @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11    @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    @*/
15    void sumAndMax(int[] a) {
16        sum = 0;
17        max = 0;
18        int k = 0;
19
20        /*@ loop_invariant
21        @ 0 <= k && k <= a.length
22        @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23        @ && (k == 0 ==> max == 0)
24        @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25        @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26        @ && sum <= k * max;
27        @
28        @ assignable sum, max;
29        @ decreases a.length - k;
30        @*/
31        while(k < a.length) {
32            if(max < a[k]) {
33                max = a[k];
34            }
35            sum += a[k];
36            k++;
37        }
38    }
39 }
40

```

Show Postcondition/Assignable

Proof has been pruned: one open goal remains.
Show log

Key 2.11.0
About

File View Proof Options Origin Tracking
Run CVCS, Princess, Z3
Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@4:49:20 PM

SumAndMaxSumAndMaxsumAndMax

Proof Search Strategy

Proof

Proof Tree

0: OPEN GOAL

Show taclet info (inner nodes only)

Sequent

Current Goal

precondition ϕ

```

wellFormed(heap)
 $\wedge$  self = null
 $\wedge$  self.<created> = TRUE
 $\wedge$  SumAndMax::exactInstance(self) = TRUE
 $\wedge$  (a = null  $\vee$  a.<created> = TRUE)
 $\wedge$  measuredByEmpty
 $\wedge$  (  $\forall$  int i; (0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)  $\rightarrow$  0  $\leq$  a[i])
 $\wedge$  (self.<inv>  $\wedge$  a = null))

```

```

- {heapAtPre:=heap || _a:=a}
\<{
exc=null;try {
self.sumAndMax(_a)@SumAndMax;
} catch (java.lang.Throwable e) {
exc=e;
}
}> (  $\forall$  int i;
( 0  $\leq$  i  $\wedge$  i < a.length  $\wedge$  inInt(i)
 $\rightarrow$  a[i]  $\leq$  self.max)
 $\wedge$  ( ( a.length > 0
 $\rightarrow$   $\exists$  int i;
( 0  $\leq$  i
 $\wedge$  i < a.length
 $\wedge$  inInt(i)
 $\wedge$  self.max = a[i])
 $\wedge$  ( self.sum
= (int)(bsum(int i);(0, a.length, a[i]))
 $\wedge$  ( self.sum
 $\leq$  javaMulInt(a.length, self.max)
 $\wedge$  self.<inv>)))
 $\wedge$  exc = null
 $\wedge$   $\forall$  Field f;
 $\forall$  java.lang.Object o;
( (o, f)  $\in$  {(self, SumAndMax::$sum)
U {(self, SumAndMax::$max)}}
 $\vee$  o = null
 $\wedge$  o.<created>@heapAtPre = TRUE
 $\vee$  o.f = o.f@heapAtPre))

```

program p

postcondition ψ

Source

```

class SumAndMax {
1
2
3   int sum;
4   int max;
5
6
7   /* normal_behaviour
8   @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
9   @ assignable sum, max;
10  @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
11  @ ensures (a.length > 0
12  @ ==> (\existsits int i; 0 <= i && i < a.length; max == a[i]));
13  @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
14  @ ensures sum <= a.length * max;
15  @*/
16  void sumAndMax(int[] a) {
17      sum = 0;
18      max = 0;
19      int k = 0;
20
21      /* loop_invariant
22      @ 0 <= k && k <= a.length
23      @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
24      @ && (k == 0 ==> max == 0)
25      @ && (k > 0 ==> (\existsits int i; 0 <= i && i < k; max == a[i]))
26      @ && sum == (\sum int i; 0 <= i && i < k; a[i])
27      @ && sum <= k * max;
28      @
29      @ assignable sum, max;
30      @ decreases a.length - k;
31      @*/
32      while(k < a.length) {
33          if(max < a[k]) {
34              max = a[k];
35          }
36          sum += a[k];
37          k++;
38      }
39  }
40

```

Show Postcondition/Assignable

Proof has been pruned: one open goal remains.
Show log

Key 2.11.0

File View Proof Options Origin Tracking

Run CVC5, Princess, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@4:49:20 PM

SumAndMaxSumAndMaxSumAndMax

Proof Search Strategy

Proof

Proof Tree

0: OPEN GOAL

Sequent

Current Goal

```

wellFormed(heap)
  precondition  $\phi$ 
   $\wedge \neg self = null$ 
   $\wedge self.<created> = TRUE$ 
   $\wedge SumAndMax::exactInstance(self) = TRUE$ 
   $\wedge (a = null \vee \forall a.<created> = TRUE)$ 
   $\wedge$  measuredByEmpty
   $\wedge ( \forall int\ i; (0 \leq i \wedge i < a.length \wedge inInt(i) \rightarrow 0 \leq a[i])$ 
     $\wedge (self.<inv> \wedge \neg a = null))$ 
   $\neg (heapAtPre:=heap \parallel \_a:=a)$ 
   $\wedge \{$ 
    exc=null; try {
      self.sumAndMax( $\_a$ )
    } catch (java.lang.Exception e) {
      exc=e;
    }
  }
   $\wedge \{$ 
     $\forall int\ i;$ 
    (  $0 \leq i \wedge i < a.length \rightarrow a[i] \leq sum$ 
       $\wedge ( ( a.length > 0 \rightarrow \exists int\ i;$ 
        (  $0 \leq i \wedge i < a.length \wedge inInt(i) \wedge a[self.max] = (int)(bsum(int\ i;)(0, a.length, a[i]))$ 
           $\wedge ( self.sum = (int)(bsum(int\ i;)(0, a.length, a[i]))$ 
             $\wedge ( self.sum \leq javaMulInt(a.length, self.max) \wedge self.<inv>))$ 
           $\wedge exc = null$ 
           $\wedge \forall Field\ f;$ 
             $\forall java.lang.Object\ o;$ 
            ( (o, f)  $\bullet$  ((self, SumAndMax::$sum) U ((self, SumAndMax::$max))
               $\wedge \neg o = null$ 
               $\wedge \neg o.<created> @ heapAtPre = TRUE$ 
               $\wedge o.f = o.f @ heapAtPre))$ 
        )
      )
    )
  }

```

postcondition ψ

Source

```

class SumAndMax {
  int sum;
  int max;

  /* normal behaviour
  @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
  @ assignable sum, max;
  @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
  @ ensures (a.length > 0
    ==> (\existsists int i; 0 <= i && i < a.length; max == a[i]));
  @ ensures (\sum int i; 0 <= i && i < a.length; a[i]);
  @ ensures sum <= a.length * max;
  ] a (
    int k <= a.length
    \forall int i; 0 <= i && i < k; a[i] <= max)
    0 ==> max == 0)
    ==> (\existsists int i; 0 <= i && i < k; max == a[i]))
    (\sum int i; 0 <= i && i < k; a[i])
    && sum <= k * max;
    @
    @ assignable sum, max;
    @ decreases a.length - k;
    */
    while(k < a.length) {
      if(max < a[k]) {
        max = a[k];
      }
      sum += a[k];
      k++;
    }
  }
}

```

$\phi \rightarrow \langle p \rangle \psi$

Show Postcondition/Assignable

Show log

Proof has been pruned: one open goal remains.

Part 1: Interaction on Source Code Level

Key 2.11.0
⌵ ⌵ ⌵

File View Proof Options Origin Tracking
About

Run CVC5, Princess, Z3
⏪ ⏩
📁 📄 📧 📧 📧 📧 📧
Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@4:49:20 PM

SumAndMaxSumAndMaxsumAndMax

Proof Search Strategy

Proof

Proof Tree

0: OPEN GOAL

Show tactic info (inner nodes only)

Sequent

Current Goal

```

=>
wellFormed(heap)
^ ~self = null
^ self.<created> = TRUE
^ SumAndMax::exactInstance(self) = TRUE
^ (a = null ∨ a.<created> = TRUE)
^ measuredByEmpty
^ ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → 0 ≤ a[i])
  ^ (self.<inv> ∧ ~a = null))
- {heapAtPre:=heap || ~a:=a}
  \<{
    exc=null; try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  }
  \> ( ∨ int i;
    ( 0 ≤ i ∧ i < a.length ∧ inInt(i)
      → a[i] ≤ self.max)
    ^ ( ( a.length > 0
      → ∃ int i;
        ( 0 ≤ i
          ^ i < a.length
          ^ inInt(i)
          ^ self.max = a[i])
        ^ ( self.sum
          = (int)(bsum(int i);(0, a.length, a[i]))
          ^ ( self.sum
            ≤ javaMulInt(a.length, self.max)
            ^ self.<inv>)))
    ^ exc = null
    ^ ∨ Field f;
      ∨ java.lang.Object o;
        ( (o, f) ∈ {(self, SumAndMax::$sum)}
          ∪ {(self, SumAndMax::$max)})
        ∨ ~o = null
        ^ ~o.<created>@heapAtPre = TRUE
        ∨ o.f = o.f@heapAtPre)
  )

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures (∑sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23     @ && (k == 0 ==> max == 0)
24     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (∑sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable sum, max;
29     @ decreases a.length - k;
30     @*/
31     while(k < a.length) {
32       if(max < a[k]) {
33         max = a[k];
34       }
35       sum += a[k];
36       k++;
37     }
38   }
39 }
40

```

Show Postcondition/Assignable

Proof has been pruned: one open goal remains.
Show log

Key 2.11.0
About

File View Proof Options Origin Tracking
Run CVCS, Princess, Z3
Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@4:49:20 PM

SumAndMaxSumAndMaxsumAndMax

Proof Search Strategy

Proof

Proof Tree

0: OPEN GOAL

Show taclet info (inner nodes only)

Sequent

Current Goal

Auto Pilot Full Auto Pilot Ctrl-Shift-V
 Auto Pilot (Preparation Only) Ctrl-Shift-D
 SMT Preparation Ctrl-Shift-Y
Finish Symbolic Execution Ctrl-Shift-X
 Transcendentals

```

^ SUMANDMAX::excinstance (SEIT) = TRUE
^ (a = null ∨ a.<created> = TRUE)
^ measuredByEmpty
^ ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → 0 ≤ a[i])
  ^ (self.<inv> ∧ ~a = null))
- {heapAtPre:=heap || ~a:=a}
  \<{
    exc=null;try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc=e;
    }
  }
  \> ( ∨ int i;
    ( 0 ≤ i ∧ i < a.length ∧ inInt(i)
      → a[i] ≤ self.max)
    ^ ( ( a.length > 0
      → ∃ int i;
        ( 0 ≤ i
          ^ i < a.length
          ^ inInt(i)
          ^ self.max = a[i])
        ^ ( self.sum
          = (int)(bsum(int i);(0, a.length, a[i]))
          ^ ( self.sum
            ≤ javaMulInt(a.length, self.max)
            ^ self.<inv>)))
    ^ exc = null
    ^ ∨ Field f;
      ∨ java.lang.Object o;
        ( (o, f) ∈ ((self, SumAndMax::$sum)
          ∪ ((self, SumAndMax::$max))
          ∨ ~o = null
          ^ ~o.<created>@heapAtPre = TRUE
          ∨ o.f = o.f@heapAtPre))
  )

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7     @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11              ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21       @ 0 <= k && k <= a.length
22       @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23       @ && (k == 0 ==> max == 0)
24       @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25       @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26       @ && sum <= k * max;
27       @
28       @ assignable sum, max;
29       @ decreases a.length - k;
30       @*/
31     while(k < a.length) {
32       if(max < a[k]) {
33         max = a[k];
34       }
35       sum += a[k];
36       k++;
37     }
38   }
39 }
40

```

Proof has been pruned: one open goal remains.
Show log

KEY 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax

Proof Search Strategy

Goals

Proof

Info

Proof

- Null Referen
- 523:Clo
- Index Out
- 521:Clo
- Null Referen
- 449:Close
- Null Reference
- 447:Closed g
- Index Out of Bc
- 445:Closed g
- if x_5 false
- Normal Executi
- Normal Exec
- Normal Ex
- CUT: k
- CUT: k
- Null Referen
- 2169:Cl
- Null Referen
- 2171:Close
- Index Out of
- 2240:Close
- Null Reference
- 2242:Closed
- Null Reference (_a =
- 2333:Closed goal
- Index Out of Bounds
- 2397:Closed goal
- if x_2 false
- 361:OPEN GOAL
- Null Reference (_a = null)
- 2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
  ( i ≥ 0 ∧ i < a.length
  → a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
    ≤ self.max@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
∧ ( { a.length > 0
    → ∃ int i;
      ( i ≥ 0
      ∧ i < a.length
      ∧ a[i]@heap[self.sum := 0]
        [self.max := 0]
        [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0)]

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23     @ && (k == 0 ==> max == 0)
24     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable sum, max;
29     @ decreases a.length - k;
30     @*/
31     while(k < a.length)
32       if(max < a[k]) {
33         max = a[k];
34       }
35       sum += a[k];
36       k++;
37     }
38   }
39 }
40

```

Normal Execution (_a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

Key 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax]

Proof Search Strategy

Goals

Proof

Info

Proof

Null Refer

523:Clo

Index Out

521:Clo

Null Referen

449:Close

Null Reference

447:Closed g

Index Out of Bc

445:Closed g

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_

CUT: k_

Null Refer

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Closed

Null Reference (_a =

2333:Closed goal

Index Out of Bounds

2397:Closed goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
→
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum
:= 0]
[self.max := 0]
[anon( {self, SumAndMax::$max}
U {self, SumAndMax::$sum}),
and
anon_heap_LOOP_0])
≤ self.max@heap[self
.sum := 0]
[self
.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)])
∧ ( ( a.length > 0
→ ∃ int i;
( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]

```

Source

```

SumAndMax.java
1 class SumAndMax {
2
3     int sum;
4     int max;
5
6     /*@ normal_behaviour
7     @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11    @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    @*/
15    void sumAndMax(int[] a) {
16        sum = 0;
17        max = 0;
18        int k = 0;
19
20        /*@ loop_invariant
21        @ 0 <= k && k <= a.length
22        @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23        @ && (k == 0 ==> max == 0)
24        @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25        @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26        @ && sum <= k * max;
27        @
28        @ assignable sum, max;
29        @ decreases a.length - k;
30        @*/
31        while(k < a.length)
32            if(max < a[k]) {
33                max = a[k];
34            }
35            sum += a[k];
36            k++;
37        }
38    }
39 }
40

```

Normal Execution (_a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

What is to prove?

KEY 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax]

Proof Search Strategy

Goals

Proof

Info

Null Referen

523:Clo

Index Out

521:Clo

Null Referen

449:Close

447:Close

Index Out of Bc

445:Close

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_

CUT: k_

Null Referen

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Close

Null Reference (_a =

2333:Closed goal

Index Out of Bounds

2397:Closed goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```

bsum(int i;){0,
  k_0,
  a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( ((self, SumAndMax::$max))
    U ((self, SumAndMax::$sum)),
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
  ( i ≥ 0 ∧ i < a.length
  → a[i]@heap[self.sum
    := 0]
    [self.max := 0]
    [anon( ((self, SumAndMax::$max))
      U ((self, SumAndMax::$sum)),
      anon_heap_LOOP_0)]
    and
    [self.sum := 0]
    [self.max := 0]
    [anon( ((self, SumAndMax::$max))
      U ((self, SumAndMax::$sum)),
      anon_heap_LOOP_0)]
  ≤ self.max@heap[self
    := 0]
    [self.max := 0]
    [anon( ((self, SumAndMax::$max))
      U ((self, SumAndMax::$sum)),
      anon_heap_LOOP_0)]
}
A ( ( a.length > 0
  → ∃ int i;
    ( i ≥ 0
      ∧ i < a.length
      ∧ a[i]@heap[self.sum := 0]
        [self.max := 0]
        [anon( ((self, SumAndMax::$max))
          U ((self, SumAndMax::$sum)),
          anon_heap_LOOP_0)]
    )
  )

```

Source

```

SumAndMax.java
1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max):
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int i = 0;
19
20     /*@ loop_invariant
21     @ 0 <= k && k <= a.length
22     @ \forallall int i; 0 <= i && i < k; a[i] <= max
23     @ k == 0 ==> max == 0
24     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26     @ && sum <= k * max;
27     @
28     @ assignable sum, max;
29     @ decreases a.length - k;
30     @*/
31     while(k < a.length)
32       if(max < a[k]) {
33         max = a[k];
34       }
35       sum += a[k];
36       k++;
37     }
38   }
39 }
40

```

Normal Execution (_a != null)

Show log

What is to prove?

Wrong specification?

KEY 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax

Proof Search Strategy

Goals

Proof

Info

Proof

Null Refer

523:Clo

Index Out

521:Clo

Null Referen

449:Close

Null Reference

447:Close

Index Out of Bc

445:Close

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k

CUT: k

Null Refer

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Close

Null Reference (_a =

2333:Closed goal

Index Out of Bounds

2397:Closed goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```
bsum(int i;){0,
  k_0,
  a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( ((self, SumAndMax::$max))
    U ((self, SumAndMax::$sum)),
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( ((self, SumAndMax::$max))
  U ((self, SumAndMax::$sum)),
  anon_heap_LOOP_0)]
and
anon_heap_LOOP_0]
≤ self.max@heap[self.sum := 0]
[self.max := 0]
[anon( ((self, SumAndMax::$max))
  U ((self, SumAndMax::$sum)),
  anon_heap_LOOP_0)]
}
A ( ( a.length > 0
→ ∃ int i;
( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( ((self, SumAndMax::$max))
  U ((self, SumAndMax::$sum)),
  anon_heap_LOOP_0)]

```

Source

```
SumAndMax.java
1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int i = 0;
19     /*@ loop_invariant
20     @ 0 <= k && k <= a.length
21     @ \forallall int i; 0 <= i && i < k; a[i] <= max)
22     @ k == 0 ==> max == 0)
23     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
24     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
25     @ sum <= k * max;
26     @*/
27     @ assignable sum, max;
28     @ decreases a.length - k;
29     @*/
30     /*@
31     while(k < a.length)
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39
40
```

Normal Execution (_a != null)

Show log

What is to prove?
Wrong specification?
Source code bug?

KEY 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax]

Proof Search Strategy

Goals

Proof

Info

Proof

Null Refer

523:Clo

Index Out

521:Clo

Null Referen

449:Close

Null Reference

447:Closed g

Index Out of Bc

445:Closed g

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_

CUT: k_

Null Refer

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Closed

Null Reference (_a =

2333:Closed goal

Index Out of Bounds

2397:Closed goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Sequent

```
bsum(int i;){0,
  k_0,
  a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
  U {(self, SumAndMax::$sum)},
  anon_heap_LOOP_0)]
and
self.sum := 0]
≤ self.max@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
  U {(self, SumAndMax::$sum)},
  anon_heap_LOOP_0)]
A ( ( a.length > 0
→ ∃ int i;
( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
  U {(self, SumAndMax::$sum)},
  anon_heap_LOOP_0)]

```

Source

```
SumAndMax.java
1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max):
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int i = 0;
19     /*@ loop_invariant
20     @ 0 <= k && k <= a.length
21     @ \forallall int i; 0 <= i && i < k; a[i] <= max)
22     @ k == 0 ==> max == 0)
23     @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
24     @ && sum == (\sum int i; 0 <= i && i < k; a[i])
25     @ && sum <= k * max;
26     @*/
27     and
28     @ assignable sum, max;
29     decreases a.length - k;
30     while (i < a.length)
31     {
32       if (max < a[i])
33         max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39
40
```

Normal Execution (_a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

What is to prove?
Wrong specification?
Source code bug?
Prover needs help?

Key 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax

Proof Search Strategy

Goals

Proof

Info

Proof

Null Referen

523:Clo

Index Out

521:Clo

Null Referen

449:Close

Null Reference

447:Close

Index Out of Bc

445:Close

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_

CUT: k_

Null Referen

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Close

Null Reference (_a =

2333:Close goal

Index Out of Bounds

2397:Close goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Close goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Sequent

```

bsum(int i;){0,
  k_0,
  a[i]@heap[self.sum := 0]
  [self.max := 0]
  [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
  ( i ≥ 0 ∧ i < a.length
  → a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0)]
    ≤ self.max@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0)]
  )
∧ ( { a.length > 0
  → ∃ int i;
    ( i ≥ 0
    ∧ i < a.length
    ∧ a[i]@heap[self.sum := 0]
      [self.max := 0]
      [anon( {(self, SumAndMax::$max)}
        U {(self, SumAndMax::$sum)},
        anon_heap_LOOP_0)]
    )
  )

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20   /*@ loop_invariant
21    @ 0 <= k && k <= a.length
22    @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23    @ && (k == 0 ==> max == 0)
24    @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25    @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26    @ && sum <= k * max;
27    @
28    @ assignable sum, max;
29    @ decreases a.length - k;
30    @*/
31   while(k < a.length)
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39
40

```

Normal Execution (_a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

Key 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax

Proof Search Strategy

Goals

Proof

Info

Proof

Null Referen

523:Clo

Index Out

521:Clo

Null Referen

449:Close

Null Reference

447:Close g

Index Out of Bc

445:Close g

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_

CUT: k_

Null Referen

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Close

Null Reference (_a =

2333:Close goal

Index Out of Bounds

2397:Close goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Close goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_0),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]
≤ self.max@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]
∧ ( ( a.length > 0
→ ∃ int i;
( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]

```

valid Java heap

Source

```

1 class SumAndMax {
2
3     int sum;
4     int max;
5
6     /*@ normal_behaviour
7     @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11    @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    @*/
15    void sumAndMax(int[] a) {
16        sum = 0;
17        max = 0;
18        int k = 0;
19
20        /*@ loop_invariant
21        @ 0 <= k && k <= a.length
22        @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23        @ && (k == 0 ==> max == 0)
24        @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25        @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26        @ && sum <= k * max;
27        @
28        @ assignable sum, max;
29        @ decreases a.length - k;
30        @*/
31        while(k < a.length)
32            if(max < a[k]) {
33                max = a[k];
34            }
35            sum += a[k];
36            k++;
37        }
38    }
39 }
40

```

Normal Execution (_a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

Key 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax

Proof Search Strategy

Goals

Proof

Info

Proof

Null Refer

523:Clo

Index Out

521:Clo

Null Referen

449:Close

Null Reference

447:Close g

Index Out of Bc

445:Close g

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_

CUT: k_

Null Refer

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Close

Null Reference (_a =

2333:Close goal

Index Out of Bounds

2397:Close goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Close goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_A),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∀ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∀ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]
≤ self.max@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]
∧ ( { a.length > 0
→ ∃ int i;
( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]

```

valid Java heap
type information

?

Source

```

1 class SumAndMax {
2
3     int sum;
4     int max;
5
6     /*@ normal_behaviour
7     @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11    @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    @*/
15    void sumAndMax(int[] a) {
16        sum = 0;
17        max = 0;
18        int k = 0;
19
20        /*@ loop_invariant
21        @ 0 <= k && k <= a.length
22        @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23        @ && (k == 0 ==> max == 0)
24        @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25        @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26        @ && sum <= k * max;
27        @
28        @ assignable sum, max;
29        @ decreases a.length - k;
30        @*/
31        while(k < a.length)
32            if(max < a[k]) {
33                max = a[k];
34            }
35            sum += a[k];
36            k++;
37        }
38    }
39 }
40

```

Normal Execution (_a != null)

Show log

Key 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax]

Proof Search Strategy

Goals

Proof

Info

Proof

Null Refer

523:Clo

Index Out

521:Clo

Null Referen

449:Close

Null Reference

447:Closed g

Index Out of Bc

445:Closed g

if x_5 false

Normal Executi

Normal Exec

Normal Ex

CUT: k_

CUT: k_

Null Refer

2169:Cl

Null Referen

2171:Close

Index Out of

2240:Close

Null Reference

2242:Closed

Null Reference (_a =

2333:Closed goal

Index Out of Bounds

2397:Closed goal

if x_2 false

361:OPEN GOAL

Null Reference (_a = null)

2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Sequent

```

bsum(int i;){0,
    k_0,
    a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
    U {(self, SumAndMax::$sum)},
    anon_heap_LOOP_0)]
= self.sum@anon_heap_LOOP_0,
self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
wellFormed(anon_heap_LOOP_A),
wellFormed(heap),
self.<created> = TRUE,
SumAndMax::exactInstance(self) = TRUE,
a.<created> = TRUE,
measuredByEmpty,
a.length ≥ 0,
∃ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
⇒
k_0 < a.length,
self = null,
a = null,
∃ int i;
( i ≥ 0 ∧ i < a.length
→ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]
≤ self.max@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]
∧ ( ( a.length > 0
→ ∃ int i;
( i ≥ 0
∧ i < a.length
∧ a[i]@heap[self.sum := 0]
[self.max := 0]
[anon( {(self, SumAndMax::$max)}
U {(self, SumAndMax::$sum)},
anon_heap_LOOP_0)]

```

valid Java heap
type information
no termination witness

?

Source

```

SumAndMax.java
1 class SumAndMax {
2
3     int sum;
4     int max;
5
6     /*@ normal_behaviour
7     @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8     @ assignable sum, max;
9     @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10    @ ensures (a.length > 0
11    @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12    @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13    @ ensures sum <= a.length * max;
14    @*/
15    void sumAndMax(int[] a) {
16        sum = 0;
17        max = 0;
18        int k = 0;
19
20        /*@ loop_invariant
21        @ 0 <= k && k <= a.length
22        @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23        @ && (k == 0 ==> max == 0)
24        @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25        @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26        @ && sum <= k * max;
27        @
28        @ assignable sum, max;
29        @ decreases a.length - k;
30        @*/
31        while(k < a.length)
32            if(max < a[k]) {
33                max = a[k];
34            }
35            sum += a[k];
36            k++;
37        }
38    }
39 }
40

```

Normal Execution (_a != null)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Show log

KEY 2.11.0

File View Proof Options Origin Tracking

Run Princess, CVCS, Z3

Layouts: Default Load Layout Save Layout Reset Layout

Loaded Proofs

Proofs

.with model src@0:15:22 PM

SumAndMax[SumAndMax:sumAndMax]

Proof Search Strategy

Goals

Proof

Info

Proof

- Null Refer
- 523:Clo
- Index Out
- 521:Clo
- Null Referen
- 449:Close
- Null Reference
- 447:Closed g
- Index Out of Bc
- 445:Closed g
- if x_5 false
- Normal Executi
- Normal Exec
- Normal Ex
- CUT: k_
- CUT: k_
- Null Refer
- 2169:Cl
- Null Referen
- 2171:Close
- Index Out of
- 2240:Close
- Null Reference
- 2242:Closed
- Null Reference (_a =
- 2333:Closed goal
- Index Out of Bounds
- 2397:Closed goal
- if x_2 false
- 361:OPEN GOAL
- Null Reference (_a = null)
- 2244:Closed goal

how Axiom Satisfiability

Show tactic info (inner nodes only)

Strategy: Applied 64 rules (0.0 sec), closed 1 goal, 1 remaining

Sequent

```

bsum(int i;){0,
  k_0,
  a[i]@heap[self.sum := 0
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0)]
  = self.sum@anon_heap_LOOP_0,
  self.max@anon_heap_LOOP_0 * k_0 ≥ self.sum@anon_heap_LOOP_0,
  wellFormed(anon_heap_LOOP_A),
  wellFormed(heap),
  self.<created> = TRUE,
  SumAndMax::exactInstance(self) = TRUE,
  a.<created> = TRUE,
  measuredByEmpty,
  a.length ≥ 0,
  ∃ int i; (i < a.length ∧ i ≥ 0 → a[i] ≥ 0)
  ⇒
  k_0 < a.length,
  self = null,
  a = null,
  ∃ int i;
  ( i ≥ 0 ∧ i < a.length
  → a[i]@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0)]
  ≤ self.max@heap[self.sum := 0]
    [self.max := 0]
    [anon( {(self, SumAndMax::$max)}
      U {(self, SumAndMax::$sum)},
      anon_heap_LOOP_0)]
  ∧ ( { a.length > 0
    → ∃ int i;
      ( i ≥ 0
        ∧ i < a.length
        ∧ a[i]@heap[self.sum := 0]
          [self.max := 0]
          [anon( {(self, SumAndMax::$max)}
            U {(self, SumAndMax::$sum)},
            anon_heap_LOOP_0)]

```

valid Java heap
type information
no termination witness
heap encoding

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7    @ requires (\forallall int i; 0 <= i && i < a.length; 0 <= a[i]);
8    @ assignable sum, max;
9    @ ensures (\forallall int i; 0 <= i && i < a.length; a[i] <= max);
10   @ ensures (a.length > 0
11   @ ==> (\exists int i; 0 <= i && i < a.length; max == a[i]));
12   @ ensures sum == (\sum int i; 0 <= i && i < a.length; a[i]);
13   @ ensures sum <= a.length * max;
14   @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20   /*@ loop_invariant
21    @ 0 <= k && k <= a.length
22    @ && (\forallall int i; 0 <= i && i < k; a[i] <= max)
23    @ && (k = 0 ==> max == 0)
24    @ && (k > 0 ==> (\exists int i; 0 <= i && i < k; max == a[i]))
25    @ && sum == (\sum int i; 0 <= i && i < k; a[i])
26    @ && sum <= k * max;
27    @
28    @ assignable sum, max;
29    @ decreases a.length - k;
30    @*/
31   while(k < a.length)
32     if(max < a[k]) {
33       max = a[k];
34     }
35     sum += a[k];
36     k++;
37   }
38 }
39 }
40

```

Normal Execution (a != null)

Show log

?

← →

Progress so far

“Integrating Source Code, Specification and Proof State into a Single Interactive View for the Deductive Verification Tool KeY” (Master’s Thesis, Mike Schwörer)

Idea: Represent a goal (sequent) of the proof as JML.

Progress so far

“Integrating Source Code, Specification and Proof State into a Single Interactive View for the Deductive Verification Tool KeY” (Master’s Thesis, Mike Schwörer)

Idea: Represent a goal (sequent) of the proof as JML.

- 1 Take initial PO and assign origins/categories to the terms
- 2 Transform correctly under rule applications
- 3 Render the new view:

Input: Sequent with origin/category tags, Java/JML

Output: Source code with additional JML assume/assert statements placed

Progress so far

“Integrating Source Code, Specification and Proof State into a Single Interactive View for the Deductive Verification Tool KeY” (Master’s Thesis, Mike Schwörer)

Idea: Represent a goal (sequent) of the proof as JML.

- 1 Take initial PO and assign origins/categories to the terms
- 2 Transform correctly under rule applications
- 3 Render the new view:
Input: Sequent with origin/category tags, Java/JML
Output: Source code with additional JML assume/assert statements placed

Assumptions

- Symbolic execution has finished (no modalities).
- All updates are applied.
- Restrictions to allowed programs (e.g., no for loops, only return + variable, ...).

Loaded Proofs Sequent

Loaded Proofs
Proofs
-with model Part_1@3:07:05 PM
CaesarChiffre|CaesarChiffre:calcCh

ExtSourceView ((DEBUG))
Goals
Info Proof Search Strategy
Exploration Steps Proof
Proof
Proof Tree
0:OPEN GOAL

Cannot transform formula with modalities. - Finish symbolic execution to continue

```
CaesarChiffre.java
19 @ ensures (\forallall int i; 0 <= i && i < valuesOutput.length; ( valuesInput[i] + offset <= 'Z' ==> ( valuesOutput[i] == (valuesInput[i] + offset ) ) );
20 @ ensures (\forallall int i; 0 <= i && i < valuesOutput.length; ( valuesInput[i] + offset > 'Z' ==> ( valuesOutput[i] == (valuesInput[i] + offset - 26 ) ) );
21 @
22 @ ensures (\forallall int i; 0 <= i && i < valuesOutput.length; 'A' <= valuesOutput[i] && valuesOutput[i] <= 'Z');
23 @
24 @ ensures result == valuesInput.length;
25 @
26 @ assignable valuesInput[*], valuesOutput[*];
27 @*/
28 int calcChiffre(int offset) {
29
30     int loopidx = 0;
31
32     convertToUpper();
33
34     /*@
35     @ loop_invariant 0 <= loopidx;
36     @ loop_invariant loopidx <= valuesInput.length;
37     @
38     @ loop_invariant ( \forallall int i; 0 <= i && i < loopidx; ( valuesInput[i] + offset <= 'Z' ==> ( valuesOutput[i] == (valuesInput[i] + offset - 26 ) ) );
39     @ loop_invariant ( \forallall int i; 0 <= i && i < loopidx; ( valuesInput[i] + offset > 'Z' ==> ( valuesOutput[i] == (valuesInput[i] + offset ) ) );
40     @
41     @ loop_invariant ( \forallall int i; 0 <= i && i < loopidx; 'A' <= valuesOutput[i] && valuesOutput[i] <= 'Z' );
42     @
43     @ decreases valuesInput.length - loopidx;
44     @
45     @ assignable valuesOutput[*];
46     @*/
47     while (loopidx < valuesInput.length){
48
49         if (valuesInput[loopidx] <= 'Z' - offset) {
50             int tmp1 = valuesInput[loopidx] + offset;
51             valuesOutput[loopidx] = (char)tmp1;
52
53         } else {
54
55             int tmp2 = valuesInput[loopidx] + offset - 26;
56             valuesOutput[loopidx] = (char)tmp2;
57
58         }
59
60         loopidx++;
61     }
62 }
```

Symbolic Execution and Simplification
Symbolic Execution, Simplification, and Close Provable Goals
Close If Provable
Cut on this term (cut_direct)
Cut
Split
Split, and Close Provable Goals
Hide this term
Insert Hidden (0 items)
Instantiate Quantifier

Show taclet info (inner nodes only)

Show Postcondition/Assignable

Loaded Proofs

Loaded Proofs

Proofs

- with model Part 1@3:07:05 PM
- CaesarChiffre[CaesarChiffre:calcCh

ExtSourceView (DEBUG)

Goals

Info Proof Search Strategy

Exploration Steps Proof

Proof

- Valid
- variant
- ion (x_arr_1 != null)
- cution (x_arr_1 != null)
- e
- al Execution (x_arr_2 != null)
- _5 true
- _5 false
- Normal Execution (x_arr_3 != null)
- Normal Execution (x_arr_5 != null)
- Case 1
 - Case 1
 - Case 1
 - Case 2
 - 18711:OPEN GO
- Case 2
- Case 2
- Case 2
- Null Reference (x_arr_5 = null)
- Index Out of Bounds (x_arr_5 != null)
- Null Reference (x_arr_3 = null)
- Index Out of Bounds (x_arr_3 != null)
- reference (x_arr_2 = null)
- Out of Bounds (x_arr_2 != null, but
- e
- nce (x_arr_1 = null)
- (x_arr = null)
- vertToUpper)

Show taclet info (inner nodes only)

```
Source
CaesarChiffre.java
33
34
35 /*@
36 @ loop_invariant 0 <= loopidx;
37 @ loop_invariant loopidx <= valuesInput.length;
38 @
39 @ loop_invariant ( \forallall int i; 0 <= i && i < loopidx; ( valuesInput[i] + offset <= 'Z' ) ==> ( valuesOutput[i] == (valuesInput[i] + offset - 26 ) ) );
40 @ loop_invariant ( \forallall int i; 0 <= i && i < loopidx; ( valuesInput[i] + offset > 'Z' ) ==> ( valuesOutput[i] == (valuesInput[i] + offset ) ) );
41 @
42 @ loop_invariant ( \forallall int i; 0 <= i && i < loopidx; 'A' <= valuesOutput[i] && valuesOutput[i] <= 'Z' );
43 @
44 @ decreases valuesInput.length - loopidx;
45 @
46 @ assignable valuesOutput[*];
47 @*/
48
49 /* assume \forallall int i; ((i < (void(valuesInput).length)) && (0 <= i)) ==> ('A' <= valuesInput[i] && valuesInput[i] <= 'Z');
50 /* assume !(void(valuesInput)[loopidx] <= (90 + (offset * -1)));
51 while (loopidx < valuesInput.length){
52
53     if (valuesInput[loopidx] <= 'Z' - offset){
54         int tmp1 = valuesInput[loopidx] + offset;
55         valuesOutput[loopidx] = (char)tmp1;
56
57     } else {
58
59         /* assume ( \forallall int i; 0 <= i && i < loopidx; ( valuesInput[i] + offset <= 'Z' ) ==> ( valuesOutput[i] == (valuesInput[i] + offset - 26 ) ) );
60         /* assume ( \forallall int i; 0 <= i && i < loopidx; ( valuesInput[i] + offset > 'Z' ) ==> ( valuesOutput[i] == (valuesInput[i] + offset ) ) );
61         /* assume \forallall int i; 0 <= i && i < loopidx; 'A' <= valuesOutput[i] && valuesOutput[i] <= 'Z' );
62         int tmp2 = valuesInput[loopidx] + offset - 26;
63         valuesOutput[loopidx] = (char)tmp2;
64
65     }
66
67     /* assume offset >= 0;
68     /* assume offset < 26;
69     /* assume 0 <= loopidx;
70
71     loopidx++;
72     /* assert ( \forallall int i; 0 <= i && i < loopidx; ( valuesInput[i] + offset > 'Z' ) ==> ( valuesOutput[i] == (valuesInput[i] + offset ) ) );
73
74 }
75
76 return valuesOutput.length;
77
78 }
79
80 /*@ normal_behaviour
81 @
82 @ requires valuesInput.length > 0;
83
84 Normal Execution (x_arr_5 != null)
```

Loaded Proofs
Proofs
with model Part_1@3:07:05 PM
CaesarChiffre(CaesarChiffre:calcChiff

ExtSourceView (DEBUG)
Goals
Info Proof Search Strategy
Exploration Steps Proof
Proof
Valid
variant
ion (x_arr_1 = null)
ution (x_arr_2 != null)
e
al Execution (x_arr_2 != null)
_5 true
_5 false
Normal Execution (x_arr_3 != null)
Normal Execution (x_arr_5 != null)
Case 1
Case 1
Case 1
Case 2
18711:OPEN GO
Case 2
Case 2
Null Reference (x_arr_5 = null)
Index Out of Bounds (x_arr_5 != null)
Null Reference (x_arr_3 = null)
Index Out of Bounds (x_arr_3 != null)
reference (x_arr_2 = null)
Out of Bounds (x_arr_2 != null, but
e
nce (x_arr_1 = null)
(x_arr = null)
vertToUpper)

```
    + (self.valuesInput@heap)[i]@heapAfter_convertToUpper[anon(self.valuesOutput
        anon_heap_LOOP)]
\forall int i;
  ( i < loopidx_0 & i >= 0
  -> offset
    + (self.valuesInput@heap)[i]@heapAfter_convertToUpper[anon(self.valuesOutput
        anon_heap_LOOP)]
  > 90
  -> (self.valuesOutput@heap)[i]@heapAfter_convertToUpper[anon(self.valuesOutput
        anon_heap_LOOP)]
  = offset
    + (self.valuesInput@heap)[i]@heapAfter_convertToUpper[anon(self.valuesOutput
        anon_heap_LOOP)]
\forall int i;
  ( i < loopidx_0 & i >= 0
  -> (self.valuesOutput@heap)[i]@heapAfter_convertToUpper[anon(self.valuesOu
        anon_heap_LOOP
    & (self.valuesOutput@heap)[i]@heapAfter_convertToUpper[anon(self.valuesOu
        anon_heap_LOOP
    <= 90)
==>
(self.valuesInput@heap)[loopidx_0]@anon_heap_convertToUpper <= 90 + offset * -1,
self.valuesOutput = null,
self.valuesInput = null,
self.valuesOutput = self.valuesInput,
self = null,
\forall int i;
  ( i >= 0 & i < 1 + loopidx_0
  -> offset
    + self.valuesInput[i]@heapAfter_convertToUpper[anon(self.valuesOutput.*,
        anon_heap_LOOP)]
    [self.valuesOutput[loopidx_0]
  > 90
  -> self.valuesOutput[i]@heapAfter_convertToUpper[anon(self.valuesOutput.*,
        anon_heap_LOOP)]
    [self.valuesOutput[loopidx_0]
  = offset
    + self.valuesInput[i]@heapAfter_convertToUpper[anon(self.valuesOutput.*,
        anon_heap_LOOP)]
    [self.valuesOutput[loopidx_0]
```

```
CaesarChiffre.java
33
34 /*
35 @ loop_invariant 0 <= loopidx;
36 @ loop_invariant loopidx <= valuesInput.length;
37 @
38 @ loop_invariant ( \forall int i; 0 <= i && i < loopidx; { valuesInput[i] + off
39 @ loop_invariant ( \forall int i; 0 <= i && i < loopidx; { valuesInput[i] + off
40 @
41 @ loop_invariant ( \forall int i; 0 <= i && i < loopidx; 'A' <= valuesOutput[i]
42 @
43 @ decreases valuesInput.length - loopidx;
44 @
45 @ assignable valuesOutput[*];
46 e*/
47 // assume \forall int i; ((i < (void(valuesInput).length)) && (0 <= i)) ==> {
48 // assume !(void(valuesInput)[loopidx] <= {90 + (offset * -1)});
49 while (loopidx < valuesInput.length) {
50     if (valuesInput[loopidx] <= 'Z' - offset) {
51         int tmp1 = valuesInput[loopidx] + offset;
52         valuesOutput[loopidx] = (char)tmp1;
53     } else {
54
55         //@ assume ( \forall int i; 0 <= i && i < loopidx; { valuesInput[i] + off
56         //@ assume ( \forall int i; 0 <= i && i < loopidx; { valuesInput[i] + off
57         //@ assume ( \forall int i; 0 <= i && i < loopidx; 'A' <= valuesOutput[i]
58         int tmp2 = valuesInput[loopidx] + offset - 26;
59         valuesOutput[loopidx] = (char)tmp2;
60     }
61
62     //@ assume offset >= 0;
63     //@ assume offset < 26;
64     //@ assume 0 <= loopidx;
65     loopidx++;
66     //@ assert ( \forall int i; 0 <= i && i < loopidx; { valuesInput[i] + offset
67
68 return valuesOutput.length;
69
70 normal_behaviour
71
72
73
74
75
76
77
78
79
80
81
82
83
84
85
86
87
88
89
90
91
92
93
94
95
96
97
98
99
100
```

Part 2: Proof Slicing

Proof Slicing

Sequent calculus: A sequent

$$\phi_0, \dots, \phi_n \Longrightarrow \psi_0, \dots, \psi_m$$

is valid iff

$$\phi_0 \wedge \dots \wedge \phi_n \rightarrow \psi_0 \vee \dots \vee \psi_m$$

is valid.

Proof Slicing

Sequent calculus: A sequent

$$\phi_0, \dots, \phi_n \Longrightarrow \psi_0, \dots, \psi_m$$

is valid iff

$$\phi_0 \wedge \dots \wedge \phi_n \rightarrow \psi_0 \vee \dots \vee \psi_m$$

is valid.

Example proof:

$$\begin{array}{c}
 \frac{}{*} \\
 \hline
 p \Longrightarrow q, p \quad \text{close} \\
 \hline
 p, \neg q \Longrightarrow p \quad \text{notLeft} \\
 \hline
 p \wedge \neg q \Longrightarrow p \quad \text{andLeft} \\
 \hline
 \Longrightarrow (p \wedge \neg q) \rightarrow p \quad \text{impRight}
 \end{array}$$

Proof Slicing

Sequent calculus: A sequent

$$\phi_0, \dots, \phi_n \Longrightarrow \psi_0, \dots, \psi_m$$

is valid iff

$$\phi_0 \wedge \dots \wedge \phi_n \rightarrow \psi_0 \vee \dots \vee \psi_m$$

is valid.

Example proof:

$$\begin{array}{c}
 \frac{*}{\frac{\frac{\frac{p \Longrightarrow q, p}{\text{notLeft}}}{p, \neg q \Longrightarrow p}}{\text{andLeft}}}{\Longrightarrow (p \wedge \neg q) \rightarrow p} \text{impRight} \\
 \text{close}
 \end{array}$$

Proof Slicing

Sequent calculus: A sequent

$$\phi_0, \dots, \phi_n \Longrightarrow \psi_0, \dots, \psi_m$$

is valid iff

$$\phi_0 \wedge \dots \wedge \phi_n \rightarrow \psi_0 \vee \dots \vee \psi_m$$

is valid.

Example proof:

$$\begin{array}{c}
 \frac{}{*} \\
 \frac{\text{close}}{\textcircled{p} \Longrightarrow q, \textcircled{p}} \\
 \frac{\text{notLeft}}{\textcircled{p}, \neg q \Longrightarrow \textcircled{p}} \\
 \frac{\text{andLeft}}{p \wedge \neg q \Longrightarrow p} \\
 \frac{\text{impRight}}{\Longrightarrow (p \wedge \neg q) \rightarrow p}
 \end{array}$$

Proof Slicing

Sequent calculus: A sequent

$$\phi_0, \dots, \phi_n \Longrightarrow \psi_0, \dots, \psi_m$$

is valid iff

$$\phi_0 \wedge \dots \wedge \phi_n \rightarrow \psi_0 \vee \dots \vee \psi_m$$

is valid.

Example proof:

$$\begin{array}{c}
 \frac{}{*} \\
 \hline
 \text{close} \\
 \frac{\text{close}}{\text{notLeft}} \\
 \frac{\text{notLeft}}{\text{andLeft}} \\
 \frac{\text{andLeft}}{\text{impRight}} \\
 \hline
 \Longrightarrow (p \wedge \neg q) \rightarrow p
 \end{array}$$

Loaded Proofs

Proofs

Env. with no model

- ✓ projectkey

Sequent

Inner Node

```
lives(z7_0),
killed(z7_0, agatha),
lives(agatha),
lives(butler),
lives(charles),
z7_0 = charles,
forall S z8; (!lives(z8) | z8 = agatha | z8 = butler | z8 = charles),
hates(z7_0, agatha),
forall S z0; (hates(z7_0, z0) | !killed(charles, z0)),
forall S z0; (hates(butler, z0) | !killed(butler, z0)),
forall S z0; (hates(agatha, z0) | !killed(agatha, z0)),
forall S z0; (hates(charles, z0) | !killed(charles, z0)),
forall S z9; forall S z0; (hates(z9, z0) | !killed(z9, z0)),
forall S w2; (!killed(z7_0, w2) | !richer(z7_0, w2)),
forall S w2; (!killed(butler, w2) | !richer(butler, w2)),
forall S w1; forall S w2; (!killed(w1, w2) | !richer(w1, w2)),
forall S w3; (hates(agatha, w3) | !hates(charles, w3)),
w8_1 = butler,
w8_0 = butler,
forall S w4; (w4 = butler | hates(agatha, w4)),
richer(butler, agatha),
hates(butler, z7_0),
forall S w5; (hates(butler, w5) | richer(w5, agatha)),
forall S w6; (!hates(agatha, w6) | hates(butler, w6)),
forall S w7; !exists S w8; !hates(w7, w8)
==>
killed(butler, agatha),
killed(butler, butler),
killed(agatha, butler),
killed(charles, w8_2),
richer(charles, agatha),
killed(z7_0, w8_3),
hates(z7_0, w8_3),
hates(charles, w8_2),
hates(agatha, butler),
hates(butler, butler),
butler = agatha,
killed(agatha, agatha)
```

Source

No source loaded

Goals

Proof Slicing

Exploration Steps

Proof

Info

Proof Search Strategy

Proof

- 99:cut_direct
- CUT: z7_0 = charles TRUE
 - ✗ 100:One Step Simplification: 1 rule
 - ✗ 122:true_left
 - ✗ 123:applyEq
 - ✗ 124:applyEq
 - ✗ 125:applyEq
 - ✗ 126:applyEq
 - ✗ 127:applyEq
 - ✗ 128:applyEq
 - ✗ 129:applyEq
 - ✗ 130:applyEq
 - ✗ 131:applyEq
 - ✗ 132:applyEq
 - ✗ 133:applyEq
 - 134:allLeft
 - 135:replace_known_left
 - ▶ 136:One Step Simplification: 2 rules
 - 137:notLeft
 - 138:allLeft
 - 139:eqSymm
 - 140:replace_known_right
 - ▶ 141:One Step Simplification: 2 rules
 - 142:closeFalse
 - ✓ 143:Closed goal
- CUT: z7_0 = charles FALSE
 - ▶ 101:One Step Simplification: 1 rule
 - 102:cut_direct
- CUT: z7_0 = butler TRUE
 - ✗ 103:One Step Simplification: 1 rule
 - ✗ 112:true_left
 - ✗ 113:applyEq
 - ✗ 114:applyEq
 - ✗ 115:applyEq
 - ✗ 116:applyEq
 - ✗ 117:applyEq
 - ✗ 118:eqSymm
 - 119:applyEq

Loaded Proofs

Proofs

Env. with no model

- ✓ project.key
- ✓ project_slice1.proof

Sequent

Closed Goal

```
lives(z7_0),
killed(z7_0, agatha),
lives(agatha),
lives(butler),
lives(charles),
z7_0 = charles,
z7_0 = agatha | z7_0 = butler | true,
forall S z8; (!lives(z8) | z8 = agatha | z8 = butler | z8 = charles),
hates(charles, agatha),
forall S z0; (hates(z7_0, z0) | !killed(z7_0, z0)),
forall S z9; forall S z0; (hates(z9, z0) | !killed(z9, z0)),
forall S w2; (!killed(z7_0, w2) | !richer(z7_0, w2)),
forall S w1; forall S w2; (!killed(w1, w2) | !richer(w1, w2)),
forall S w3; (!hates(agatha, w3) | !hates(charles, w3)),
w8_0 = butler,
false,
forall S w4; (w4 = butler | hates(agatha, w4)),
hates(butler, z7_0),
forall S w5; (hates(butler, w5) | richer(w5, agatha)),
forall S w6; (!hates(agatha, w6) | hates(butler, w6)),
forall S w7; !exists S w8; !hates(w7, w8)
==>
hates(agatha, agatha),
richer(z7_0, agatha),
hates(agatha, w8_0),
hates(butler, butler),
butler = agatha,
killed(agatha, agatha)
```

Source

No source loaded

Goals

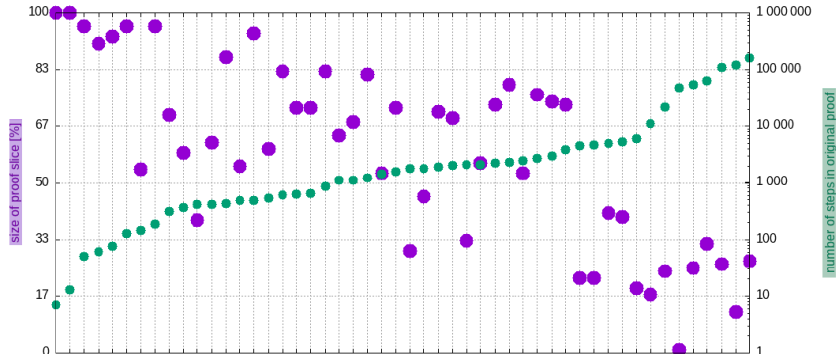
Proof Slicing

Exploration Steps

Proof

- 44:replace_known_left
- 45:One Step Simplification: 2 rules
- 46:notLeft
- 47:allLeft
- 48:replace_known_right
- 49:One Step Simplification: 1 rule
- 50:applyEq
- 51:allLeft
- 52:replace_known_right
- 53:One Step Simplification: 1 rule
- 54:allLeft
- 55:replace_known_left
- 56:One Step Simplification: 2 rules
- 57:cut_direct
- 58:CUT: z7_0 = charles TRUE
 - 58:applyEq
 - 60:allLeft
 - 61:replace_known_left
 - 62:One Step Simplification: 2 rules
 - 63:notLeft
 - 64:allLeft
 - 65:eqSymm
 - 66:replace_known_right
 - 67:One Step Simplification: 2 rules
 - 68:closeFalse
 - 69:Closed goal
- 70:CUT: z7_0 = charles FALSE
- 59:One Step Simplification: 1 rule
- 70:cut_direct
- 71:CUT: z7_0 = butler TRUE
 - 71:applyEq
 - 73:close
 - 74:Closed goal
- 72:CUT: z7_0 = butler FALSE
 - 72:One Step Simplification: 1 rule
 - 75:applyEq
 - 76:close
 - 77:Closed goal

Evaluation



- Often, very large parts of proofs could be removed.
- Trend: The larger the proof, the larger the percentage.
- Most of the removed steps are normalizations of formulas which are never used later on.

Part 3: Proof Caching

Proof Caching

Motivation: Finding the correct and provable specification is often an iterative process.

Proof Caching

Motivation: Finding the correct and provable specification is often an iterative process.

Observation: If $\Gamma \Longrightarrow \Delta$ is valid, then $\Gamma, E \Longrightarrow \Delta, Z$ is also valid (*).

Proof Caching

Motivation: Finding the correct and provable specification is often an iterative process.

Observation: If $\Gamma \Longrightarrow \Delta$ is valid, then $\Gamma, E \Longrightarrow \Delta, Z$ is also valid (*).

(*) Under some restrictions:

- The Java code referred to must be the same.
- Both must use the same prover settings for semantics.
- The same added rules must be present.

Proof Caching

Motivation: Finding the correct and provable specification is often an iterative process.

Observation: If $\Gamma \Longrightarrow \Delta$ is valid, then $\Gamma, E \Longrightarrow \Delta, Z$ is also valid (*).

(*) Under some restrictions:

- The Java code referred to must be the same.
- Both must use the same prover settings for semantics.
- The same added rules must be present.

Ongoing work:

- Which sequents should be in the cache?
- Extend the caching beyond a single run of KeY.
- Relax the above conditions.

Key2.111.0
About

File View Proof Options Origin Tracking
Layouts: Default Load Layout Save Layout Reset Layout
Exploration Mode Hide Justification

Loaded Proofs

Proofs

.with model src:7:05:05 PM

✓ SumAndMax[SumAndMax:sumAndMax[]],JML normal_behavior operation c

Goals Proof Slicing Exploration Steps

Proof Info Proof Search Strategy

Proof

Proof Tree

- Invariant Initially Valid
- Invariant Preserved and Used

Sequent

Inner Node

```

=>
wellFormed(heap)
  A ~self = null
  A self.<created> = TRUE
  A SumAndMax::exactInstance(self) = TRUE
  A (a = null ∨ a.<created> = TRUE)
  A measuredByEmpty
  A ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → 0 ≤ a[i])
    A (self.<inv> ∧ a = null))
- {heapAtPre:=heap || _a:=a}
  \<{
    exc = null;
    try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc = e;
    }
  } \> ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → a[i] ≤ self.max)
  A ( a.length > 0
    → int i;
      (0 ≤ i ∧ i < a.length ∧ inInt(i) ∧ self.max = a[i])
    A (self.sum ≤ a.length * self.max ∧ self.<inv>))
  A exc = null
  A ∨ Field f;
  ∨ java.lang.Object o;
  ( (o, f) ∈ {(self, SumAndMax::$sum)}
    ∪ {(self, SumAndMax::$max)}
  ∨ ~o = null
    A ~o.<created>@heapAtPre = TRUE
    ∨ o.f = o.f@heapAtPre))

```

Source

SumAndMax.java

```

1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /*@ normal_behaviour
7     @ requires (∀forall int i; 0 <= i && i < a.length; 0 <= a
8     @ assignable sum, max;
9     @ ensures (∀forall int i; 0 <= i && i < a.length; a[i] <=
10    @ ensures a.length > 0
11    @ ==> (∃exists int i; 0 <= i && i < a.length; max
12    @ //ensures sum == (∑sum int i; 0 <= i && i < a.length; a
13    @ ensures sum <= a.length * max;
14    @*/
15   void sumAndMax(int[] a) {
16     sum = 0;
17     max = 0;
18     int k = 0;
19
20     /*@ loop_invariant
21       @ 0 <= k && k <= a.length
22       @ && (∀forall int i; 0 <= i && i < k; a[i] <= max)
23       @ && (k == 0 ==> max == 0)
24       @ && (k > 0 ==> (∃exists int i; 0 <= i && i < k; max =
25       @ //&& sum == (∑sum int i; 0 <= i && i < k; a[i])
26       @ && sum <= k * max;
27       @
28       @ assignable sum, max;
29       @ decreases a.length - k;
30       @*/
31     while(k < a.length) {
32       if(max < a[k]) {
33         max = a[k];
34       }
35       sum += a[k];
36       k++;
37     }
38   }
39
40 }

```

Show Postcondition/Assignable

javac (0)

Key 2.11.0

File View Proof Options Origin Tracking

Load Example... Load... Reload Edit Last Opened File Save... Save Proof as Bundle... Quicksave Quickload Proof Management Load User-Defined Tactics... Prove Recent Files Exit

Proof Tree

- Invariant Initially Valid
- Invariant Preserved and Used

Sequent

Inner Node

```
wellFormed(heap)
  A ~self = null
  A self.<created> = TRUE
  A SumAndMax::exactInstance(self) = TRUE
  A (a = null ∨ a.<created> = TRUE)
  A measuredByEmpty
  A ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → 0 ≤ a[i])
    A (self.<inv> ∧ a = null))
- {heapAtPre:=heap || _a:=a}
  \<{
    exc = null;
    try {
      self.sumAndMax(_a)@SumAndMax;
    } catch (java.lang.Throwable e) {
      exc = e;
    }
  }> ( ∨ int i; (0 ≤ i ∧ i < a.length ∧ inInt(i) → a[i] ≤ self.max)
  A ( a.length > 0
    → int i;
      (0 ≤ i ∧ i < a.length ∧ inInt(i) ∧ self.max = a[i])
    A (self.sum ≤ a.length * self.max ∧ self.<inv>))
  A exc = null
  A ∨ Field f;
    ∨ java.lang.Object o;
      ( (o, f) ∈ {(self, SumAndMax::$sum)
        ∪ {(self, SumAndMax::$max)}}
    ∨ ~o = null
      A ~o.<created>@heapAtPre = TRUE
      ∨ o.f = o.f@heapAtPre)
```

Source

SumAndMax.java

```
1 class SumAndMax {
2
3   int sum;
4   int max;
5
6   /* normal behaviour
7   @ requires (∀forall int i; 0 <= i && i < a.length; 0 <= a
8   @ assignable sum, max;
9   @ ensures (∀forall int i; 0 <= i && i < a.length; a[i] <=
10  @ ensures (a.length > 0
11  @ ==> (∃exists int i; 0 <= i && i < a.length; max
12  @ //ensures sum == (∑sum int i; 0 <= i && i < a.length; a
13  @ ensures sum <= a.length * max;
14  @*/
15  void sumAndMax(int[] a) {
16    sum = 0;
17    max = 0;
18    int k = 0;
19
20    /* loop invariant
21    @ 0 <= k && k <= a.length
22    @ && (∀forall int i; 0 <= i && i < k; a[i] <= max)
23    @ && (k == 0 ==> max == 0)
24    @ && (k > 0 ==> (∃exists int i; 0 <= i && i < k; max =
25    @ //&& sum == (∑sum int i; 0 <= i && i < k; a[i])
26    @ && sum <= k * max;
27    @
28    @ assignable sum, max;
29    @ decreases a.length - k;
30    @*/
31    while(k < a.length) {
32      if(max < a[k]) {
33        max = a[k];
34      }
35      sum += a[k];
36      k++;
37    }
38  }
39
40 }
```

Show Postcondition/Assignable

javac (0)

Summary

We have seen:

- a novel way for interaction with KeY on the source code level.
- “Proof Slicing” to minimize sequent calculus proofs.
- “Proof Caching” to avoid reproving the same formulas.

<https://github.com/KeYProject/key>