

# NPRG077

**TinyProlog:** Tiny declarative logic programming language

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# Logic programming

-  Declarative style - specify what, but not how
-  Programs consists of **facts and rules**
-  Evaluation by clever **inference engine**
-  **Prolog, Datalog** and basis of other systems
-  Origins in AI and **natural language**

# From inference to programming

## Type inference

- Program analysis
- Generated constraints
- Unification of types
- Infer type assignment
- Unification + substitution

## Logic programming

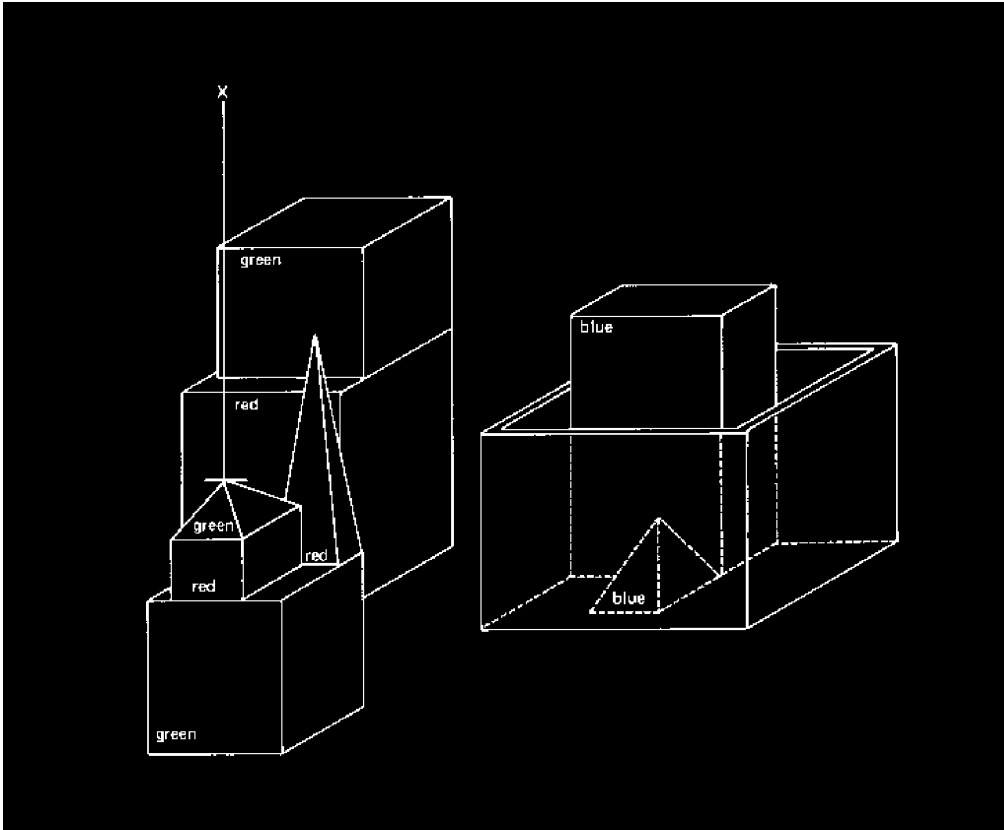
- Program evaluation
- Handwritten programs
- Unification of terms
- Infer variable assignment
- Unification + substitution

## A bit of history

Natural language processing in the late 1960s & early 1970s

SHRDLU, PLANNER

"Find a block which is taller than the one you are holding and put it into the box."



# Prolog then and now

## Alain Colmerauer, Marseilles (1972)

- Natural language processing
- Automatic theorem proving

## Fifth generation systems (1980s)

- 10 year initiative in Japan
- Epoch-making knowledge processing

## Prolog (and Datalog) today

- Used in real-world in specialized domains
- Basic of many reasoning & solving systems



# TinyProlog

Logic programming by example

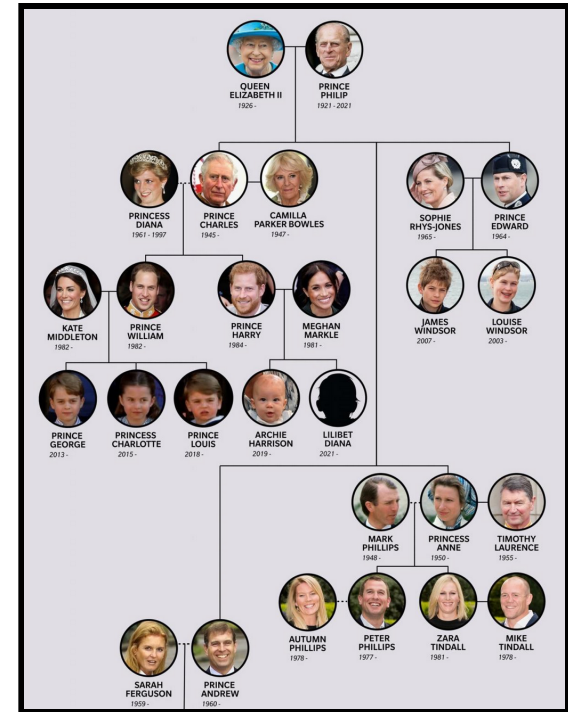
# Prolog "Hello world"

## Family tree querying

- Simple database querying
- Search for data patterns
- Grandparent (parent of a parent)  
Father (parent who is male)

## List processing

- Linked lists with "cons" and "nil"
- Matching lists with patterns
- Many functions become multi-purpose



# Demo

## Family tree and lists



# Magic squares

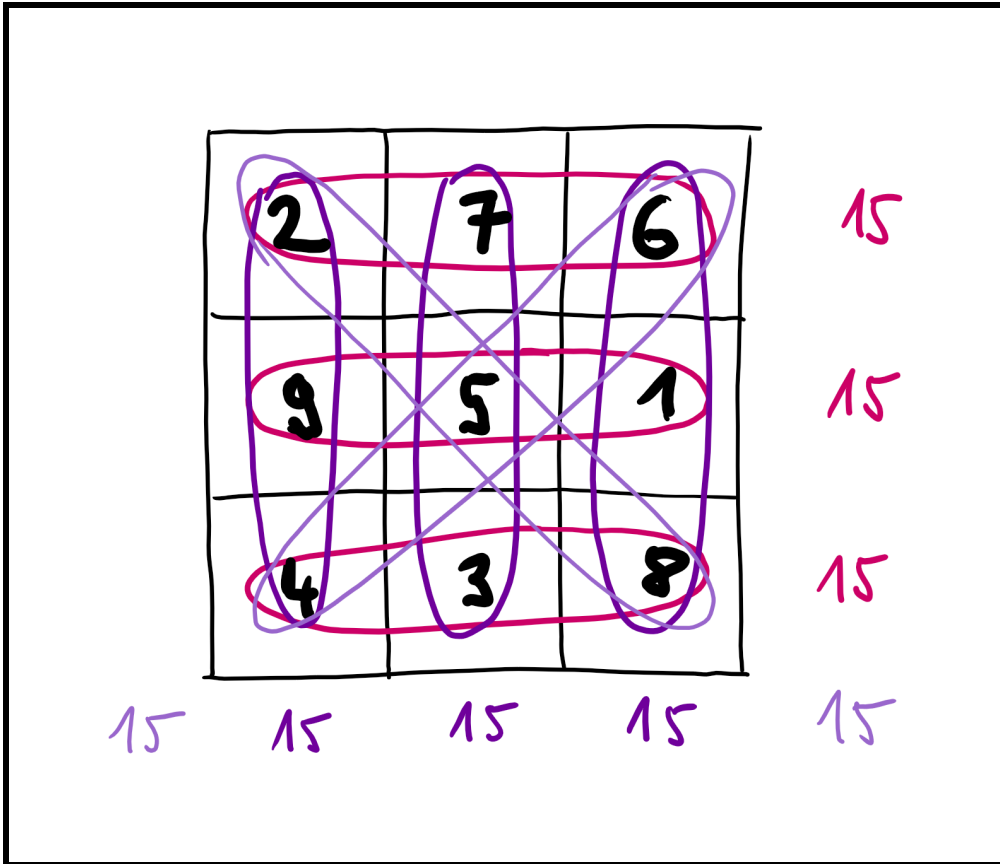
Naive method

Generate & test  
all permutations

Better approaches

Try adding only  
reasonable options

Naive is fine for us!



# Demo

## Generating magic squares

# TinyProlog

A bit of theory

# Model of knowledge

## Closed world assumption

- Only declared facts are true
- No unknown children exist!
- Shapes the semantics of Prolog

## Negation in Prolog

- **Yes** means provably true
- **No** means not provably true
- **False** only in a closed world



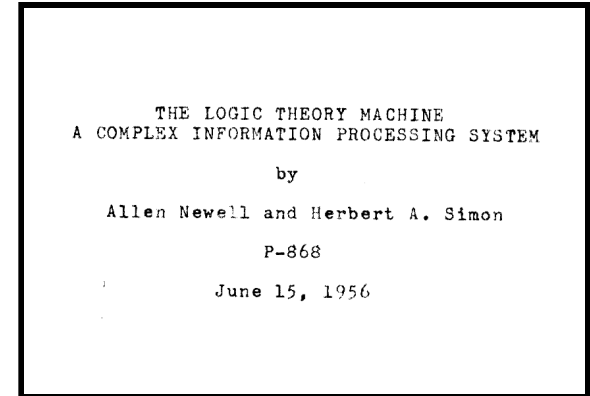
# Theory behind resolution

## Prolog programs as logic clauses

- Horn clause:  $A \leftarrow B_1 \wedge B_2 \wedge \dots \wedge B_n$
- Equivalent:  $A \vee \neg B_1 \vee \neg B_2 \vee \dots \vee \neg B_n$

## SLD resolution in Prolog

- Sound and refutation-complete resolution for Horn clauses
- Will prove 'false' if possible



# Variables in Prolog clauses

Universally quantified over formula, existentially over body

$$\forall x \forall y (\textit{grandparent}(x, y) \leftarrow \exists z (\textit{parent}(x, z) \wedge \textit{parent}(z, y)))$$

Transformed using standard logical operations

$$\forall x \forall y (\textit{grandparent}(x, y) \vee \neg \exists z (\textit{parent}(x, z) \wedge \textit{parent}(z, y)))$$

$$\forall x \forall y (\textit{grandparent}(x, y) \vee \forall z \neg (\textit{parent}(x, z) \wedge \textit{parent}(z, y)))$$

$$\forall x \forall y \forall z (\textit{grandparent}(x, y) \vee \neg \textit{parent}(x, z) \vee \neg \textit{parent}(z, y))$$

We need to use free variables when applying rule!

# Numbers

## Calculating inside Prolog

- ▶ Peano arithmetic encoded as zero & successor
- 🔌 Constraint Logic Programming (CLP) extensions
- ⬆️ CLP(Z) adds a specialized solver for integers
- 📚 CLP(B), CLP(Q), CLP(R) and more

# Cyclic terms and occurs check

## Occurs check

- Avoid terms of the form  $A = f(A)$
- Supports rational trees (cyclic terms)
- Not checking is faster, but not right



## Practical Prolog

- Some operations can fail:

$$A = 1 + A, B \text{ is } A.$$

- Checks can be turned on:

```
set_prolog_flag(occurs_check, true).
```



# Demo

Enabling occurs check

# TinyProlog

Implementation structure

# TinyProlog programs

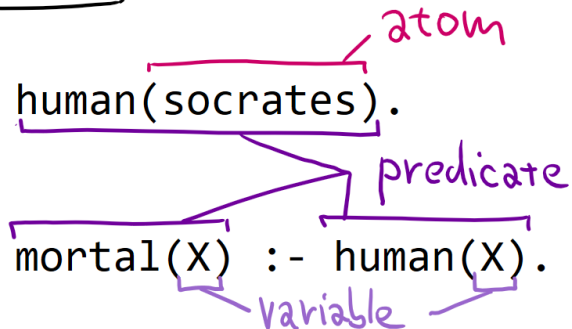
Program is a list of clauses which are:

- 1) Rules (head + body)
- 2) Facts (head)

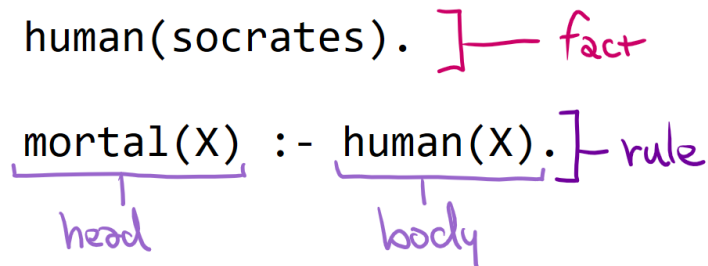
A term can be:

- 1) Variable
- 2) Atom
- 3) Predicate

term structure



program structure



```

(* Recursive term definition *)
type Term =
  | Atom of string
  | Variable of string
  | Predicate of
      string * Term list
  | Call of Term * Term list

(* Facts have empty Body *)
type Clause =
  { Head : Term
    Body : Term list }

(* Create a fact clause *)
let fact p =
  { Head = p; Body = [] }

(* Create a rule clause *)
let rule p b =
  { Head = p; Body = b }

```

# TinyProlog programs





Encoded as F# types!

## Atom vs. variable

Atom is a single data item, thing that exists.

Variable is a placeholder that we want to assign a term to.

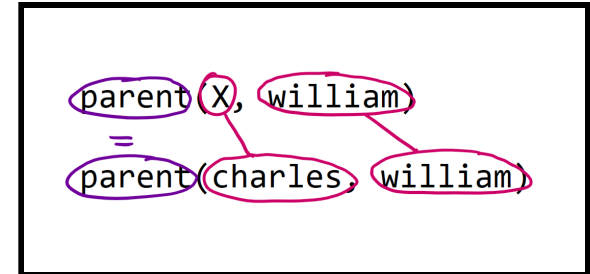
# Prolog resolution logic

-  Start with user query as the goal  
Single (or multiple) term(s) with unbound variables
-  Find applicable rule/fact by matching its head  
Unification to check if the rule can be applied
-  Generate substitution from the matching  
Substitution generated by unification process
-  Add goals based on the rule body  
Apply substitution and repeat until all goals solved

# The unification process

## Tiny implementation

- Similar to our type inference code!
- **unify** and **unifyLists** functions
- Generate substitution for variables



## Used in Prolog context

- Same 2 uses of substitution
- Occurs check done optionally
- Use fresh set of variables when reusing rules from program database!

```

let rec unifyLists l1 l2 =
  match l1, l2 with
  | [], [] ->
    (* empty substitution*)
  | h1::t1, h2::t2 ->
    match unify h1 h2 with
    | Some(s) -> (*
      1. substitution 's' to
        unify 'h1' and 'h2'
      2. now unify 't1' and 't2'
        recursively & compose
      3. if not possible, fail *)
    | _ -> (* fail *)
  | _ -> (* fail *)

and unify t1 t2 =
  match t1, t2 with
  | Atom(a1), Atom(a2) -> (* does 'a1' match 'a2'? *)
  | Variable(v), t | t, Variable(v) ->
    (* return a substitution *)
  | Predicate(p1, args1), Predicate(p2, args2) ->
    (* if p1 = p2, unify arguments recursively *)
  | _ -> None

```

## Unification logic

Split into two functions  
for better readability

**unify** matches terms

**unifyLists** matches  
two lists using **unify**

```
% Number: 0
zero

% Number: 1
one = s(zero)

% Number: 5
five = s(s(s(s(s(zero))))))

% Empty list
empty

% List [1]
cons(one, empty)

% List [1; 5]
cons(one, cons(five, empty))
```

# Adding support for numbers and lists

Nothing extra is needed!

Good enough for a tiny implementation.

Terribly inefficient and limited if you want to calculate anything!



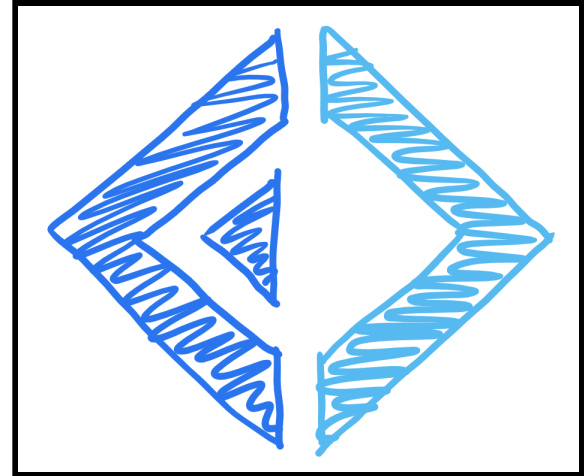
# The F# language

Useful advanced features

# Advanced F# features

## Active patterns

- Custom patterns for use in **match**
- Match number with **Odd** or **Even**
- Recognize special forms of terms
- Complete or partial patterns



## Sequence expressions

- Write code that generates a sequence of items
- Comprehensions (Haskell), generators (JS), ...
- Lazy **seq** `{..}` or eager `[..]` or arrays `[|..|]`

# Demo

## Advanced F# features

# Lab overview

TinyProlog system step-by-step

# TinyProlog - Basic tasks

1. **Implementing basic unification of terms**  
Recursively match atoms, variables and predicates
2. **Composing and applying substitutions**  
To handle multiple occurrences of a variable correctly
3. **Searching clauses & variable renaming**  
Find applicable rules and relevant facts in program
4. **Generating and proving goals recursively**  
The key trick! Generate and solve goals in a loop
5. **Adding numbers to TinyProlog**  
Representing, calculating and pretty printing

# TinyProlog - Bonus and super tasks

1. Lazy search and support for lists  
Refactoring for readability and more pretty printing
2. Generating magic squares in TinyProlog  
In which we find out how slow our implementation is :-)
3. Implementing call and functional maplist  
Adding special predicate for higher-order programming
4. Adding support for occurs checks  
If you want to make it slower and more correct
5. Implementing Prolog-style cut operator  
Super-bonus if you are into Prolog programming...

# Closing

A tiny logic programming language

# Conclusions

## A tiny declarative logic programming language

- Remarkably similar to ML type inference!
- This is not a coincidence...
- Evaluation as search, not a sequence of steps
- Much work needed to make this practical

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