

Write your own tiny programming system(s)

Programming languages and systems

Tomas Petricek, Charles University

✉ tomas@tomasp.net

✈ [@tomasp.net](https://tomasp.net)

🌐 <https://tomasp.net>

🌐 <https://d3s.mff.cuni.cz/teaching/nprg077>



Programming Languages

Programming is writing code

Formal semantics, implementation, paradigms, types

We know how to study this!

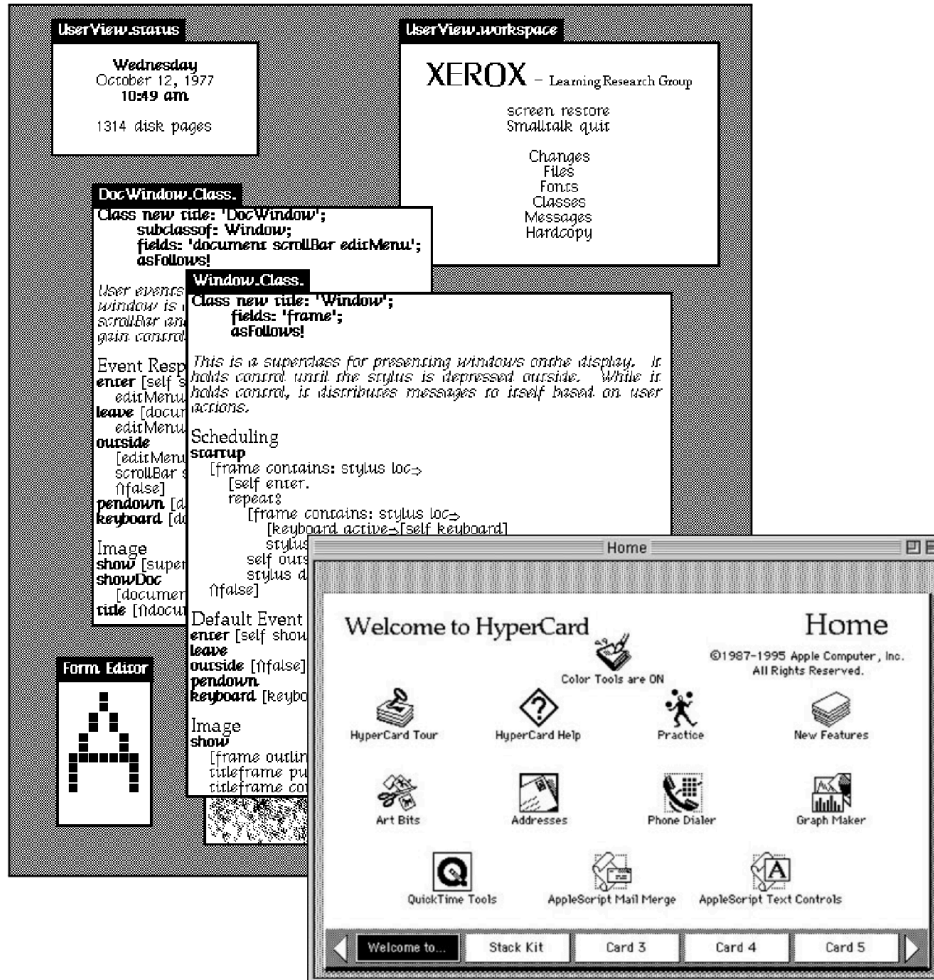
$\rightarrow \forall <: \text{Top}$		Based on System F (23-1) and simple subtyping (15-1)	
Syntax		Subtyping	$\boxed{\Gamma \vdash S <: T}$
$t ::=$	terms:	$\frac{}{\Gamma \vdash S <: S}$	(S-REFL)
x	variable	$\frac{\Gamma \vdash S <: U \quad \Gamma \vdash U <: T}{\Gamma \vdash S <: T}$	(S-TRANS)
$\lambda x:T. t$	abstraction	$\frac{}{\Gamma \vdash S <: \text{Top}}$	(S-TOP)
$t \ t$	application	$\frac{X <: T \in \Gamma}{\Gamma \vdash X <: T}$	(S-TVAR)
$\lambda X<:T. t$	type abstraction	$\frac{\Gamma \vdash T_1 <: S_1 \quad \Gamma \vdash S_2 <: T_2}{\Gamma \vdash S_1 \rightarrow S_2 <: T_1 \rightarrow T_2}$	(S-ARROW)
$t [T]$	type application	$\frac{\Gamma, X <: U_1 \vdash S_2 <: T_2}{\Gamma \vdash \forall X <: U_1. S_2 <: \forall X <: U_1. T_2}$	(S-ALL)
$v ::=$	values:	Typing	$\boxed{\Gamma \vdash t : T}$
$\lambda x:T. t$	abstraction value	$\frac{x:T \in \Gamma}{\Gamma \vdash x : T}$	(T-VAR)
$\lambda X<:T. t$	type abstraction value	$\frac{\Gamma, x:T_1 \vdash t_2 : T_2}{\Gamma \vdash \lambda x:T_1. t_2 : T_1 \rightarrow T_2}$	(T-ABS)
$T ::=$	types:	$\frac{\Gamma \vdash t_1 : T_{11} \rightarrow T_{12} \quad \Gamma \vdash t_2 : T_{11}}{\Gamma \vdash t_1 t_2 : T_{12}}$	(T-APP)
X	type variable	$\frac{\Gamma, X <: T_1 \vdash t_2 : T_2}{\Gamma \vdash \lambda X <: T_1. t_2 : \forall X <: T_1. T_2}$	(T-TABS)
Top	maximum type	$\frac{\Gamma \vdash t_1 : \forall X <: T_{11}. T_{12} \quad \Gamma \vdash T_2 <: T_{11}}{\Gamma \vdash t_1 [T_2] : [X \mapsto T_2] T_{12}}$	(T-TAPP)
$T \rightarrow T$	type of functions	$\frac{\Gamma \vdash t : S \quad \Gamma \vdash S <: T}{\Gamma \vdash t : T}$	(T-SUB)
$\forall X <: T. T$	universal type		
$\Gamma ::=$	contexts:		
$\emptyset$	empty context		
$\Gamma, x:T$	term variable binding		
$\Gamma, X <: T$	type variable binding		
Evaluation	$\boxed{t \rightarrow t'}$		
$\frac{t_1 \rightarrow t'_1}{t_1 t_2 \rightarrow t'_1 t_2}$	(E-APP1)		
$\frac{t_2 \rightarrow t'_2}{v_1 t_2 \rightarrow v_1 t'_2}$	(E-APP2)		
$\frac{t_1 \rightarrow t'_1}{t_1 [T_2] \rightarrow t'_1 [T_2]}$	(E-TAPP)		
$(\lambda X <: T_{11}. t_{12}) [T_2] \rightarrow [X \mapsto T_2] t_{12}$	(E-TAPPTABS)		
$(\lambda X : T_{11}. t_{12}) v_2 \rightarrow [X \mapsto v_2] t_{12}$	(E-APPABS)		

Programming Systems

Interacting with a stateful system

Feedback, liveness, interactive user interfaces

But how do we study this?



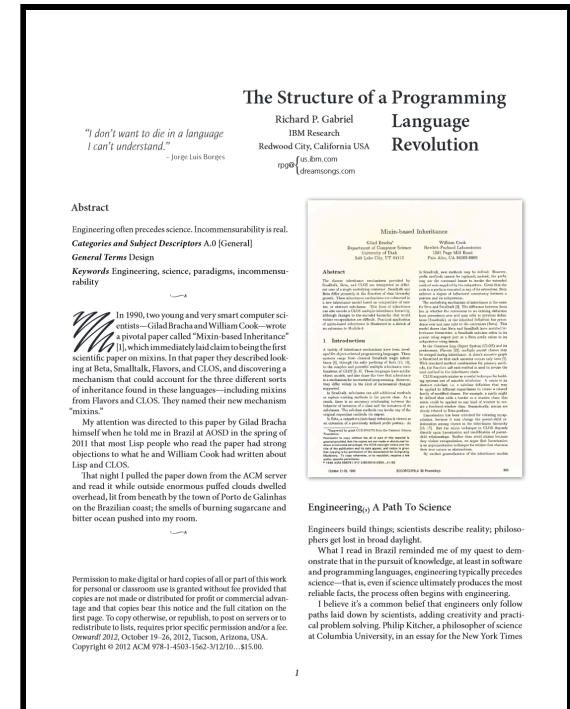
Paradigm shift in 1990s

From systems to languages

- From running system to code
- From state & interaction to semantics
- Incommensurable ways of thinking!

History of science matters!

- How did we get where we are?
- What ideas got lost along the way?
- How to recover them?



Language paradigms

- Functional programming
No mutable state, everything a function
-  Imperative programming
Mutable memory with pointers
-  Object-oriented programming
Everything an object, hides its own logic
-  Logic programming
Declare facts and use inference

Demo

Logic programming in Prolog

System interaction

- Command line programming systems
Code editor, compiler, build tools, etc.
- 🖼 Image-based programming model
Programming system is always running
- 🔄 Interactive and live programming
System provides continuous feedback
- 🔲 Incremental or reactive evaluation
Recompute on edit or when new data come

Demo

Object-orientation in Smalltalk

What really matters?

Static structure (program)

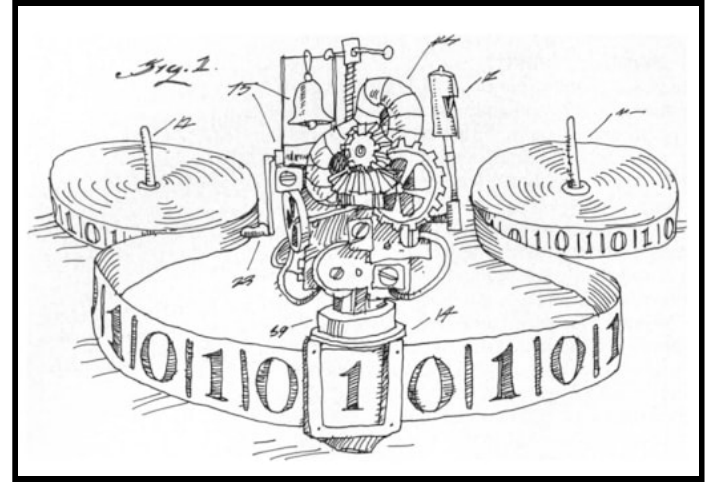
- Source code of the program
- What you have at the start

Dynamic structure (process)

- Runtime data structures
- What else do you need to run

Logic of evaluation (execution)

- How the dynamic state evolves?



Operational semantics

Standard approach
to programming
language theory

Why write small
interpreters instead?

(deref) $\langle !\ell, s \rangle \longrightarrow \langle n, s \rangle$ if $\ell \in \text{dom}(s)$ and $s(\ell) = n$

(assign1) $\langle \ell := n, s \rangle \longrightarrow \langle \text{skip}, s + \{\ell \mapsto n\} \rangle$ if $\ell \in \text{dom}(s)$

(assign2)
$$\frac{\langle e, s \rangle \longrightarrow \langle e', s' \rangle}{\langle \ell := e, s \rangle \longrightarrow \langle \ell := e', s' \rangle}$$

(seq1) $\langle \text{skip}; e_2, s \rangle \longrightarrow \langle e_2, s \rangle$

(seq2)
$$\frac{\langle e_1, s \rangle \longrightarrow \langle e'_1, s' \rangle}{\langle e_1; e_2, s \rangle \longrightarrow \langle e'_1; e_2, s' \rangle}$$

(if1) $\langle \text{if true then } e_2 \text{ else } e_3, s \rangle \longrightarrow \langle e_2, s \rangle$

(if2) $\langle \text{if false then } e_2 \text{ else } e_3, s \rangle \longrightarrow \langle e_3, s \rangle$

(if3)
$$\frac{\langle e_1, s \rangle \longrightarrow \langle e'_1, s' \rangle}{\langle \text{if } e_1 \text{ then } e_2 \text{ else } e_3, s \rangle \longrightarrow \langle \text{if } e'_1 \text{ then } e_2 \text{ else } e_3, s' \rangle}$$

```
(* A term like 'father(william, X)'
   consists of predicate 'father',
   atom 'william' and variable 'X' *)
type Term =
  | Atom of string
  | Variable of string
  | Predicate of string * Term list

(* A rule 'head(...) :- body.' *)
type Rule =
  { Head : Term
    Body : Term list }

(* A program is a list of rules *)
type Program = Rule list
```

Code can run!

A good way to explain the structures!

- 1) Functional data types for the static and dynamic structure
- 2) A function to model the evaluation logic