

Computer Architecture

Instructions and instruction set architecture design

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Recall: computer is a machine

Executes a program

- Linked chains of instructions stored in memory.
- Executes an instruction and moves to “next” one.
 - Does not “know” what it is doing, or “understand” the big picture.

Instructions are very simple

- Mostly operations on numbers.

Everything is encoded into numbers

- Not only the input and output data...
 - Text, images, music, 3D scene, ...
- ... but also the program being executed!

What instructions are needed?

*It is easy to see by formal-logical methods that **there exist certain [instruction sets] that are in abstract adequate to control and cause the execution of any sequence of operations...***

... The really decisive considerations from the present point of view, in electing an [instruction set], are more of a practical nature: simplicity of the equipment demanded by the [instruction set], and the clarity of its application to the actually important problems together with the speed of its handling of those problems.

– Burks, Goldstine, and von Neumann, 1947

Arithmetic operations

There must certainly be instructions for performing the fundamental arithmetic operations.

– Burks, Goldstine, and von Neumann, 1947

Arithmetic operations

Adding (two variables)

- The most basic of basic operations.

add a, b, c # a = b + c

- Add variables b and c and store result in a.
- One operation, always three variables.
 - Regularity helps make the hardware simple.

Adding three (four) variables

- Two (three) instructions needed

add a, b, c # a = b + c

add a, a, d # a = b + c + d

add a, a, e # a = b + c + d + e

Compiling assignments (1)

Simple expression

```
a := b + c;
```

```
d := a - e;
```

Corresponding MIPS assembly

```
add a, b, c           # a = b + c
```

```
sub d, a, e           # d = a - e
```

Compiling assignments (2)

Complex expression

$f := (g + h) - (i + j);$

- Compiler must break down the statement into multiple assembly instructions.

Corresponding MIPS assembly

```
add t0, g, h      # t0 = g + h
add t1, i, j      # t1 = i + k
sub f, t0, t1     # f = t0 - t1
```

- Programmer only deals with the 5 variables.
- Compiler determines where to store the (temporary) intermediate results.

Operands

Instruction operands restricted to *registers*

- Limited number of special locations in the hardware visible to programmer.
 - 32 on the MIPS architecture.
 - More than 16-32 not necessarily better. Why?
- The size of a register is limited as well.
 - 32 bits (word) on the 32-bit MIPS architecture.

Effective use of registers critical to performance

- Compiler allocates registers as necessary to hold different values at different stages of program execution.

Referring to registers on the MIPS

Register number in the instruction code

- 5 bits required to express registers 0 – 31.

Symbolic name in the assembly language

- Reflects agreed-upon usage of a register.
- $\$r0$ ($\$zero$) and $\$r31$ ($\$ra$) are special.

Name	Number	Usage	Name	Number	Usage
$\$zero$	0	The constant value 0.	$\$t8 - \$t9$	24 – 25	More temporaries.
$\$at$	1	Reserved for assembler.	$\$k0 - \$k1$	26 – 27	Reserved for OS kernel.
$\$v0 - \$v1$	2 – 3	Values of results and expressions.	$\$gp$	28	Global pointer.
$\$a0 - \$a3$	4 – 7	Function arguments.	$\$sp$	29	Stack pointer.
$\$t0 - \$t7$	8 – 15	Temporaries.	$\$fp / \$s8$	30	Frame pointer (if used).
$\$s0 - \$s7$	16 – 23	Saved registers.	$\$ra$	31	Return address.

Compiling assignments using registers

Complex expression

$f := (g + h) - (i + j);$

Corresponding MIPS assembly

- The compiler assigned variables **f**, **g**, **h**, **i**, and **j** to registers **\$s0**, **\$s1**, **\$s2**, **\$s3**, and **\$s4**.

```
add $t0, $s1, $s2      # $t0 = g + h
add $t1, $s3, $s4      # $t1 = i + k
sub $s0, $t0, $t1      # f = $t0 - $t1
```

Memory operands

Everything is primarily kept in memory

- Variables and data structures contain more data elements than there are registers in a computer.
 - Only small amount of data can be kept in registers.

Arithmetic operations only work with registers

- *Data transfer instructions* needed to transfer data between memory and registers.
- Instructions must supply the memory *address*.
- Memory is a 1-dimensional array of bytes.
 - The address serves as a zero-based index.
 - 32-bit word addresses must be aligned to 4 bytes.

Data transfer instructions

Load/store word

- **lw \$rd, imm16 (\$rs)**

$$R[rd] = M[R[rs] + \text{signext32}(\text{imm16})]$$

- **sw \$rt, imm16 (\$rs)**

$$M[R[rs] + \text{signext32}(\text{imm16})] = R[rt]$$

Load/store byte

- **lb \$rd, imm16 (\$rs)**

$$R[rd] = \text{signext32}(M[R[rs] + \text{signext32}(\text{imm16})][7:0])$$

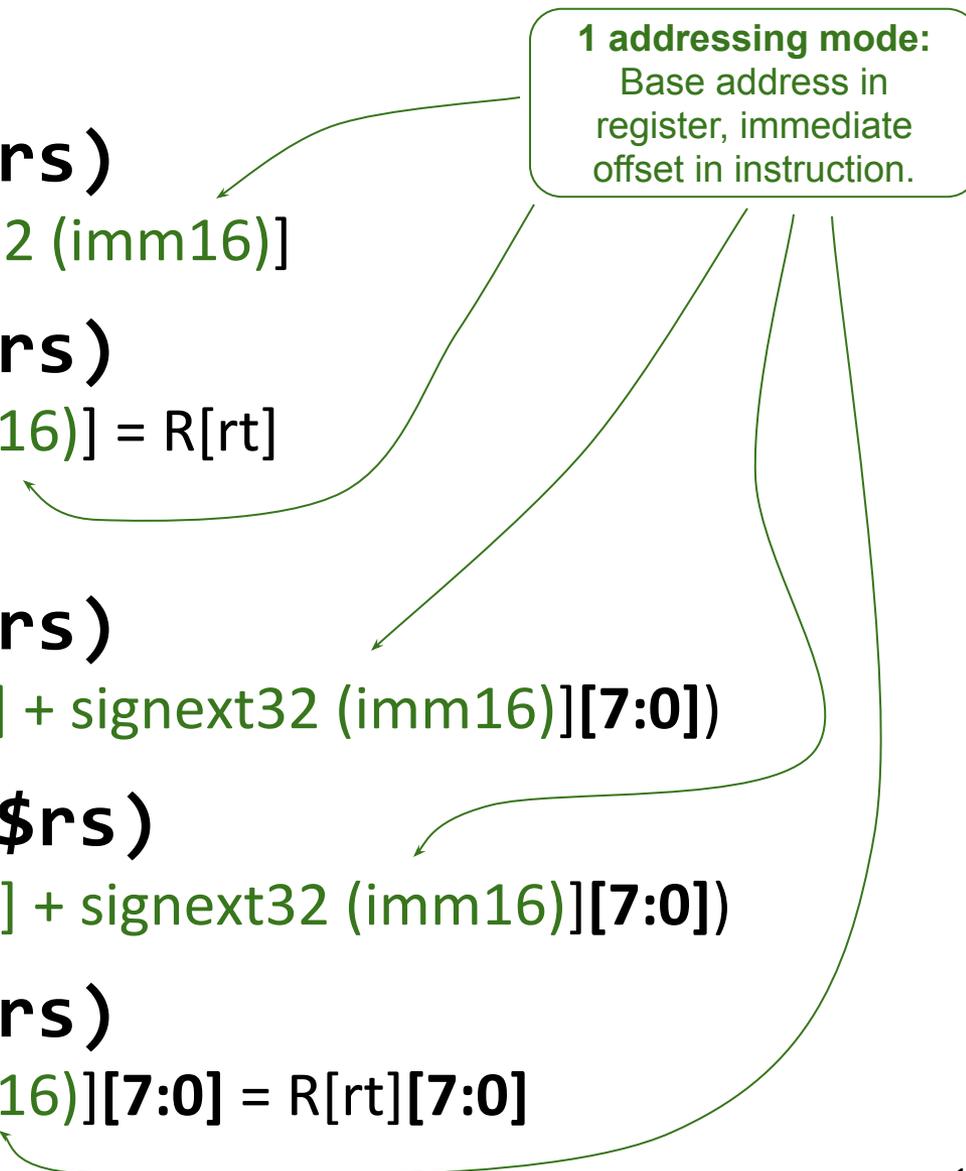
- **lbu \$rd, imm16 (\$rs)**

$$R[rd] = \text{zeroext32}(M[R[rs] + \text{signext32}(\text{imm16})][7:0])$$

- **sb \$rt, imm16 (\$rs)**

$$M[R[rs] + \text{signext32}(\text{imm16})][7:0] = R[rt][7:0]$$

1 addressing mode:
Base address in register, immediate offset in instruction.



Compiling using a memory operand

Program fragment

```
var A : array [0 .. 99] of Integer;  
g := h + A[8];
```

Corresponding MIPS assembly

- Variables **g** and **h** assigned to **\$s1** and **\$s2**.
- The base (starting) address of array **A** is in **\$s3**.
- The offset of **A[8]** is $8 \times \text{SizeOf}(\text{Integer})$

```
lw $t0, 32 ($s3)           # $t0 = A[8]  
add $s1, $s2, $t0         # g = h + A[8]
```



Compiling using load and store

Program fragment

- Single assignment, two memory operands.

```
var A : array [0 .. 99] of Integer;  
A[12] := h + A[8];
```

Corresponding MIPS assembly

- Variable **h** assigned to **\$s2**.
- The base address of array **A** is in **\$s3**.

```
lw $t0, 32 ($s3)      # $t0 = A[8]  
add $t0, $s2, $t0     # $t0 = h + A[8]  
sw $t0, 48 ($s3)     # A[12] = h + A[8]
```

Constant/immediate operands

Avoid extra memory reads for (common) constants

- Incrementing/decrementing a loop control variable or an index, initializing sums and products, ...
 - Common values: 0, 1, -1, 2, ... (constant structure sizes)

Immediate operands

- **addi \$rd, \$rs, imm16**
add immediate, $R[rd] = R[rs] + \text{signext32}(\text{imm16})$
- **li \$rd, imm32**
load immediate, $R[rd] = \text{imm32}$

Zero is special (hardwired in \$r0)

- **move \$rd, \$rs = add \$rd, \$rs, \$r0**
 $R[rd] = R[rs]$

Logical operations

Operations on bits and bit fields within words

- Isolating, setting, and clearing bits.

Bitwise operations

- **and/or/xor/nor \$rd, \$rs, \$rt**
 - not \$rd, \$rs = nor \$rd, \$rs, \$rs/\$r0
- **andi/ori/xori \$rd, \$rs, imm16**
R[rd] = R[rs] and/or/xor **zeroext32** (imm16)

Shift operations

- **sll/slr \$rd, \$rs, shamt**
shift logical left/right, R[rd] = R[rs] << / >> shamt
- **sra \$rd, \$rs, shamt**
shift arithmetic right, R[rd] = R[rs] >>> shamt

Compiling logical operations

Program fragment

```
shamt := (insn and $000007C0) shr 6;
```

Corresponding MIPS assembly

- Variables **shamt**, **insn** assigned to **\$s1**, **\$s2**.

```
andi $t0, $s2, 0x7C0      # $t0 = insn & 0x7C0  
srl  $s1, $t0, 6          # shamt = $t0 >> 6
```

Instructions for making decisions (1)

Distinguishes computer from calculator

- Choose which instructions to execute based on inputs and values created during computation.
 - Control statements in programming languages.

Conditional branches / jumps

- **beq \$rd, \$rs, addr**

branch if eq, if $R[rs] == R[rt]$ then $PC = \text{addr}$ else $PC = PC + 4$

- **bne \$rd, \$rs, addr**

branch not eq, if $R[rs] \neq R[rt]$ then $PC = \text{addr}$ else $PC = PC + 4$

Unconditional jumps

- **j addr**

jump, $PC = \text{addr}$

address
of next
instruction

Compiling if-then-else statement

Program fragment

```
if (i = j) then
    f := g + h;
else
    f := g - h;
```

- Variables **f**, **g**, **h**, **i**, and **j** assigned to registers **\$s0**, **\$s1**, **\$s2**, **\$s3**, and **\$s4**.

Corresponding MIPS assembly

```
bne $s3, $s4, Else      # (i <> j) ⇒ PC = Else
add $s0, $s1, $s2      # f = g + h
j End                   # PC = End
```

Else:

```
sub $s0, $s1, $s2      # f = g - h
```

End:

...

Compiling while loop

Program fragment

```
while (save [i] = k) do
    i := i + 1;
```

Corresponding MIPS assembly

- Variables **i**, **k** assigned to **\$s3**, **\$s5**, and the base address of array **save** is in **\$s6**.

Loop:

```
sll $t1, $s3, 2           # $t1 = i × 4
add $t1, $t1, $s6        # $t1 = @save[i]
lw $t0, 0($t1)           # $t0 = save[i]
bne $t0, $s5, End        # (save[i] <> k) ⇒ PC = End
addi $s3, $s3, 1         # i = i + 1
j Loop                    # PC = Loop
```

End:

Instructions for making decisions (2)

Set on less than

- Check all relations (together with beq/bne)

Signed variant

- **slt \$rd, \$rs, \$rt**
if $R[rs] <_s R[rt]$ then $R[rd] = 1$ else $R[rd] = 0$
- **slti \$rd, \$rs, imm16**
if $R[rs] <_s \text{signext32}(\text{imm16})$ then $R[rd] = 1$ else $R[rd] = 0$

Unsigned variant

- **sltu \$rd, \$rs, \$rt**
if $R[rs] <_u R[rt]$ then $R[rd] = 1$ else $R[rd] = 0$
- **sltiu \$rd, \$rs, imm16**
if $R[rs] <_u \text{zeroext32}(\text{imm16})$ then $R[rd] = 1$ else $R[rd] = 0$

Compiling repeat-until loop

Program fragment

```
i := 0;
repeat
    i := i + 1;
until i >= k;
```

Corresponding MIPS assembly

- Variables `i`, and `k` assigned to registers `$s3`, and `$s5`.

```
move $s3, $zero           # i = 0
```

Loop:

```
addi $s3, $s3, 1          # i = i + 1
slt  $t0, $s3, $s5        # $t0 = (i < k)
bne  $t0, $zero, Loop     # ($t0 <> 0) ⇒ PC = Loop
```

End:

Compiling for statement (1)

Program fragment

```
var
  a : array [0 .. 4] of Integer;
  s, i : integer;
begin
  s := 0;
  for i := 0 to 4 do begin
    s := s + a[i];
  end;
end.
```

Compiling for statement (2)

Corresponding MIPS assembly

```
move $s2, $zero           # s = 0
move $s1, $zero           # i = 0
j Condition             # PC = Condition
```

Body:

```
sll $t0, $s1, 2           # $t0 = i × 4
add $t0, $t0, $s0         # $t0 = @a[i]
lw $t1, 0($t0)           # $t1 = a[i]
add $s2, $s2, $t1        # s = s + a[i]
addi $s1, $s1, 1         # i = i + 1
```

Condition:

```
slti $t2, $s1, 5         # $t2 = (i < 5)
bne $t2, $zero, Body   # ($t2 <> 0) ⇒ PC = Body
```

End:

Supporting procedures/functions (1)

Fundamental tool for structuring programs

- Call from anywhere, with input parameters.
- Return to point of origin, with return value.
- One of the ways to abstraction and code reuse.

Basic steps to execute a routine

- Put parameters in a place accessible to routine.
- Transfer control to the routine code.
- Acquire storage needed for the routine.
- Perform the desired task.
- Put result in a place accessible to caller.
- Return control to point of origin.

Supporting procedures/functions (2)

Jump and link (call)

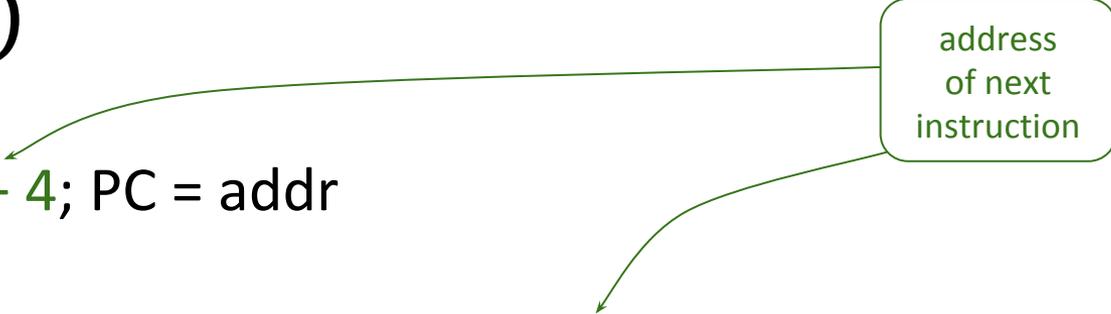
- **jal addr**

$\$ra = R[31] = PC + 4$; $PC = \text{addr}$

- **jalr \$rs**

jump and link register, $\$ra = R[31] = PC + 4$; $PC = R[rs]$

address
of next
instruction



Indirect jump / return

- **jr \$rs**

jump register, $PC = R[rs]$

Registers used for calling routines

- First four arguments passed in $\$a0 - \$a3$
- Return value passed back in $\$v0 - \$v1$
- Address where to return passed in $\$ra (\$r31)$

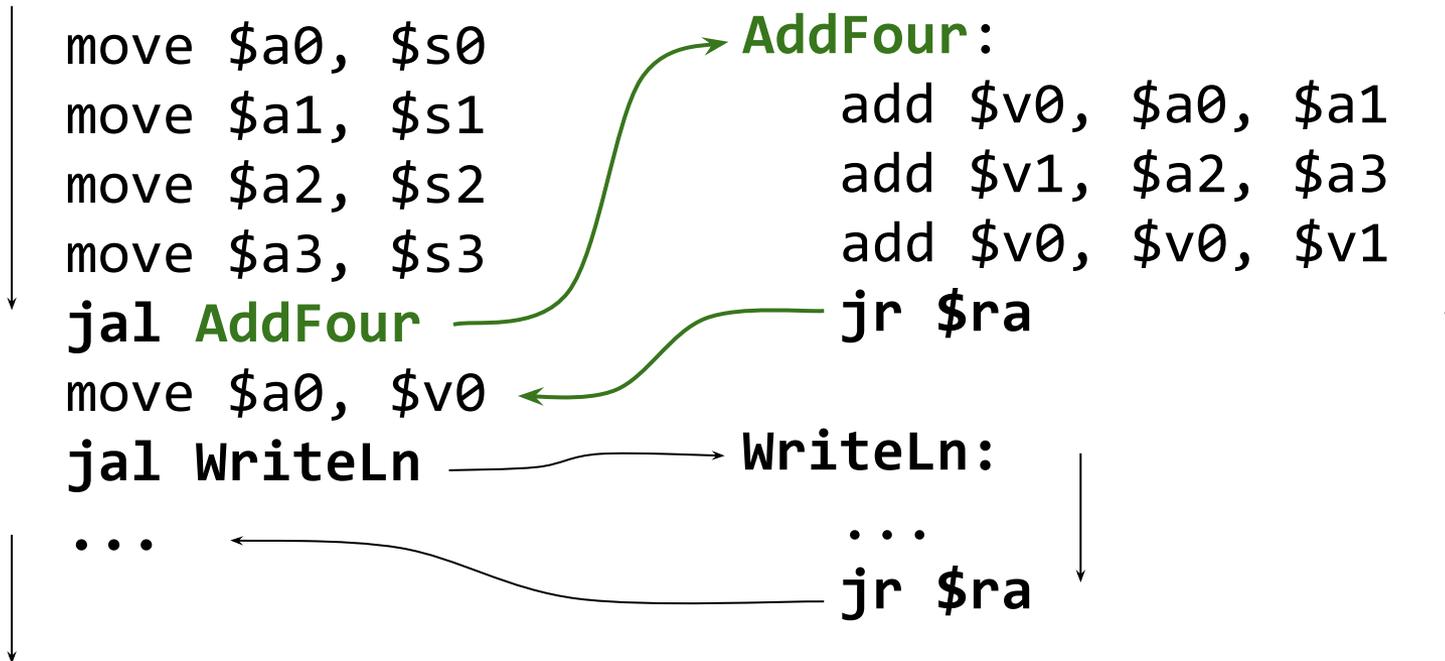
Compiling simple function call

Program fragment

```
WriteLn (AddFour (a, b, c, d));
```

Corresponding MIPS assembly

- Variables **a**, **b**, **c**, and **d** assigned to **\$s0**, **\$s1**, **\$s2**, and **\$s3**.



Supporting procedures/functions (3)

Mechanism to store register contents in memory

- Caller expects to find its own values in registers after a routine returns.
- Routine works with more values than there are registers available.

Mechanism to pass parameters through memory

- There may be more than 4 parameters.

Mechanism to return values through memory

- The returned value may be a structure.

Mechanism to acquire storage for local variables

- Loop control variables, temporaries, ...

Allocating local storage

In memory, but where?

- The location cannot be fixed, because any routine can be called multiple times.
 - A routine can call itself, either directly, or transitively.
 - A routine can be called from multiple threads.

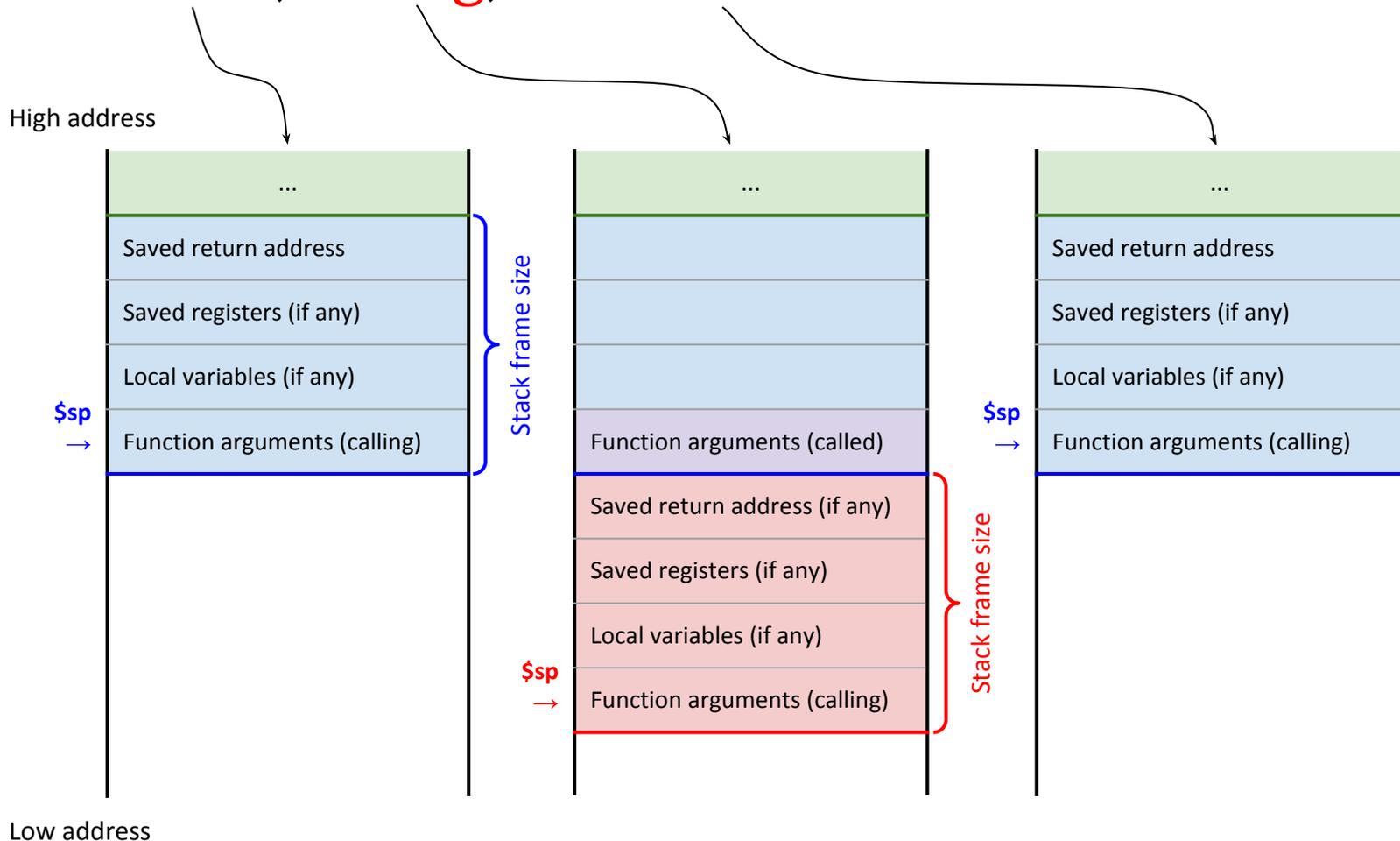
Stack data structure (Last In First Out)

- Stack pointer to the top of the stack
 - Address of last used memory location
- Push and pop operations
 - Decrement/increment stack pointer, store/retrieve value
- Access local data relative to stack pointer
- Fits the need to make nested function calls

Stack space allocation

Stack and register contents

- Before, during, and after routine call



Compiling a function call using stack

Program fragment

```
s := AddTwo (1, 2);
```

Corresponding MIPS assembly for the call

- Note: arguments would normally go only through registers.

```
addi $sp, $sp, -40    # Allocate stack frame (including space
...                  # for locals and all possible call arguments)
li $a1, 2
sw $a1, 4 ($sp)      # Put 2nd parameter on stack
li $a0, 1
sw $a0, 0 ($sp)      # Put 1st parameter on stack
jal AddTwo           # Call (jump and link) the routine
...
addi $sp, $sp, 40    # Deallocate stack frame
```

Compiling a function using stack (1)

MIPS assembly for AddTwo()

- Note: saving \$ra (\$s0, \$s1) is not strictly necessary.
- Note: arguments loaded from the caller's stack frame.

AddTwo:

```
addi $sp, $sp, -12      # Allocate stack frame
sw $ra, 8 ($sp)         # Store return address
sw $s1, 4 ($sp)         # Save register $s1
sw $s0, 0 ($sp)         # Save register $s0

lw $s0, 12 ($sp)        # Load 1st argument from stack
lw $s1, 16 ($sp)        # Load 2nd argument from stack
add $v0, $s0, $s1       # Calculate return value
```

... to be continued

Compiling a function using stack (2)

MIPS assembly for AddTwo()

... continued

```
lw $s0, 0 ($sp)      # Restore register $s0
lw $s1, 4 ($sp)      # Restore register $s1
lw $ra, 8 ($sp)      # Restore return address
addi $sp, $sp, 12    # Deallocate stack frame
jr $ra               # Return to caller
```

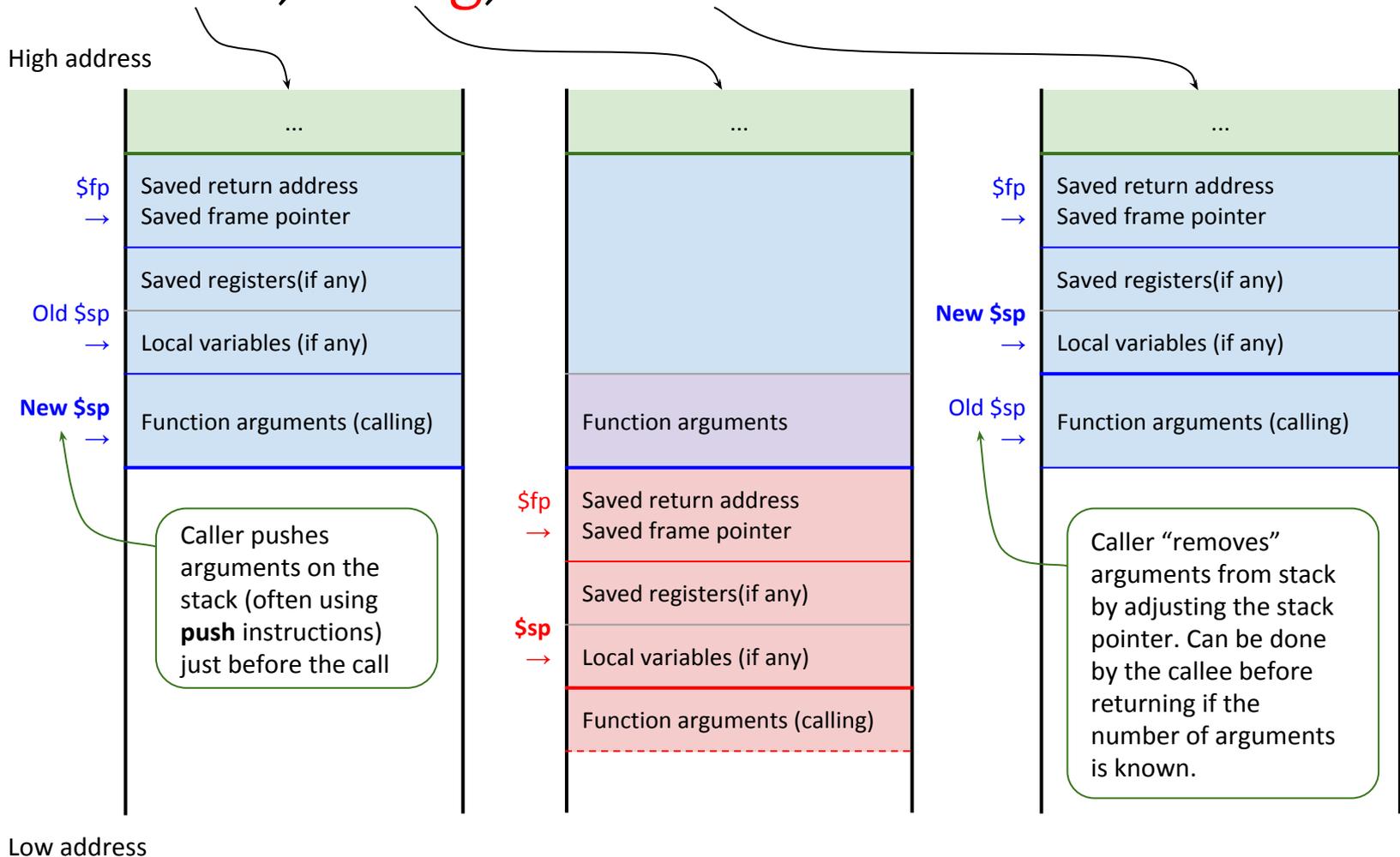
Compared to machines with HW stack support

- Stack frame (activation record) for each function is allocated as a whole, `$sp` remains fixed after allocation.
 - Not incrementally using push instructions.
- Space for all possible arguments is part of the activation record → not need to change `$sp` during execution.

Stack allocation with frame pointer

Stack and register contents

- Before, during, and after routine call



Compiling with frame pointer (1)

MIPS assembly for AddTwo()

AddTwo:

```
addi $sp, $sp, -4  
sw $ra, 0 ($sp)  
addi $sp, $sp, -4  
sw $fp, 0 ($sp)  
move $fp, $sp  
  
addi $sp, $sp, -4  
sw $s0, -4 ($fp)  
  
lw $s0, 8 ($fp)  
lw $s1, 12 ($fp)  
add $v0, $s0, $s1
```

"Push" return address on stack

"Push" old frame pointer on stack

Establish new frame pointer

Allocate the rest of the stack frame
Save \$s0 (\$fp-based addressing)

Load 1st argument (\$fp-based addressing)
Load 2nd argument (\$fp-based addressing)
Calculate return value

```
sw $ra, -4 ($sp)  
sw $fp, -8 ($sp)  
addi $fp, $sp, -8  
addi $sp, $sp, -12
```

... to be continued

Compiling with frame pointer (2)

MIPS assembly for AddTwo()

- Note: explicit stack adjustments intended to mimic function prologue (push ebp; mov esp, ebp) and epilogue (mov ebp, esp; pop ebp) typical for Intel.

... continued

```
lw $s0, -4 ($fp)      # Restore $s0 ($fp-based addressing)
move $sp, $fp         # Deallocate stack frame

lw $fp, 0 ($sp)       # "Pop" frame pointer
addi $sp, $sp, 4      #
lw $ra, 0 ($sp)       # "Pop" return address
addi $sp, $sp, 4      #
jr $ra                # Return to caller
```

MIPS instruction set

Constant length (32 bits)

- Register operations (r-type)
 - Arithmetic and logic operations, indirect jumps (to address stored in a register)
- Immediate operand instructions (i-type)
 - Arithmetic and logic operations, branching, data transfer.
- (Direct) jump instructions (j-type)
 - Unconditional jumps to immediate (absolute) address.

r-type	op (6)	rs (5)	rt (5)	rd (5)	shamt (5)	funct (6)
i-type	op (6)	rs (5)	rt (5)	signed immediate (16)		
j-type	op (6)	target (26)				

op = operation code, **rs** = source register, **rt** = source register/target register/branch condition
rd = destination register, **shamt** = shift amount, **funct** = ALU function

MIPS instruction set (2)

Good design requires (good) compromises!

- Reasonable number of instruction formats
 - Simplifies instruction decoding and execution.
 - Must not limit the instruction set expressiveness.
- Reasonable number and size of registers
 - Fast operations on data in registers.
 - Reading/writing registers must not be slow.
- Optimized for machines
 - Machine code produced by machine, not human.
 - Orthogonal operations simplify compiler design.